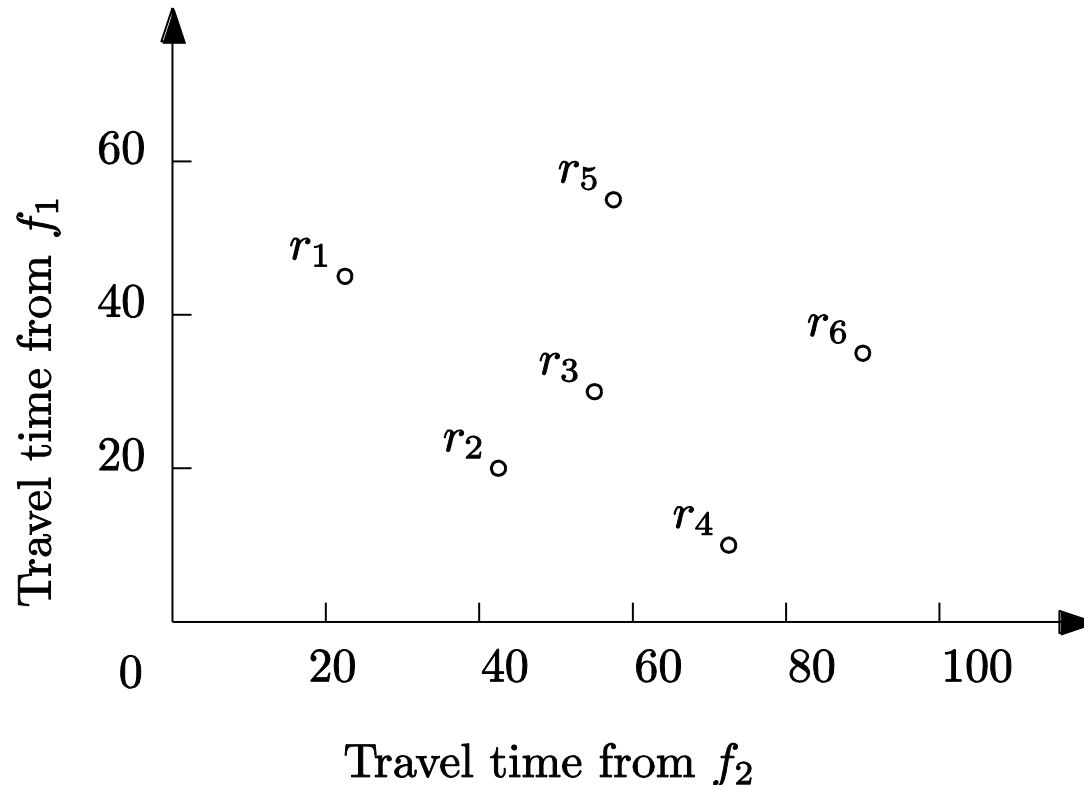


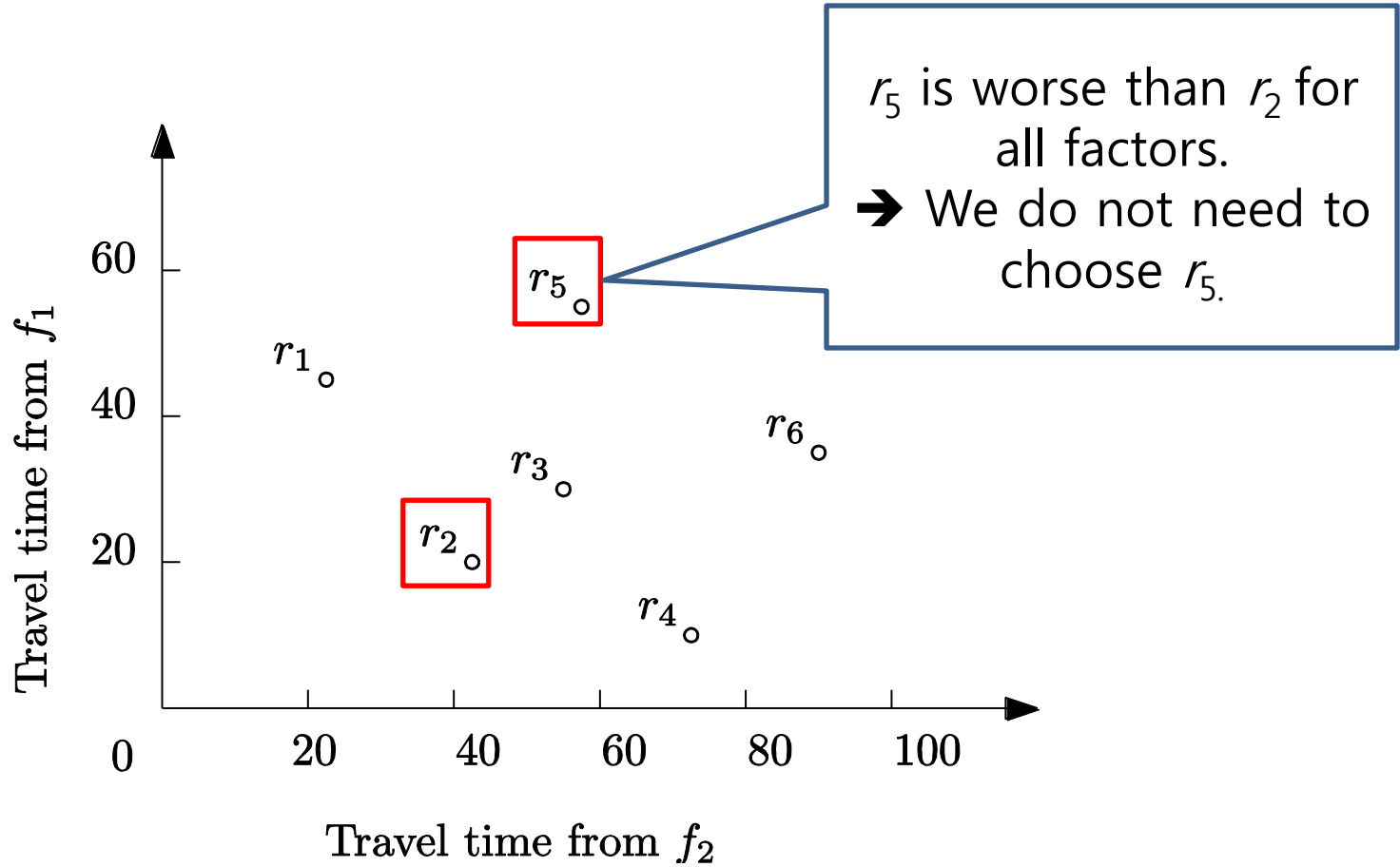
MSSQ:
Manhattan Spatial Skyline Queries

Wanbin Son
Seung-won Hwang
Hee-Kap Ahn

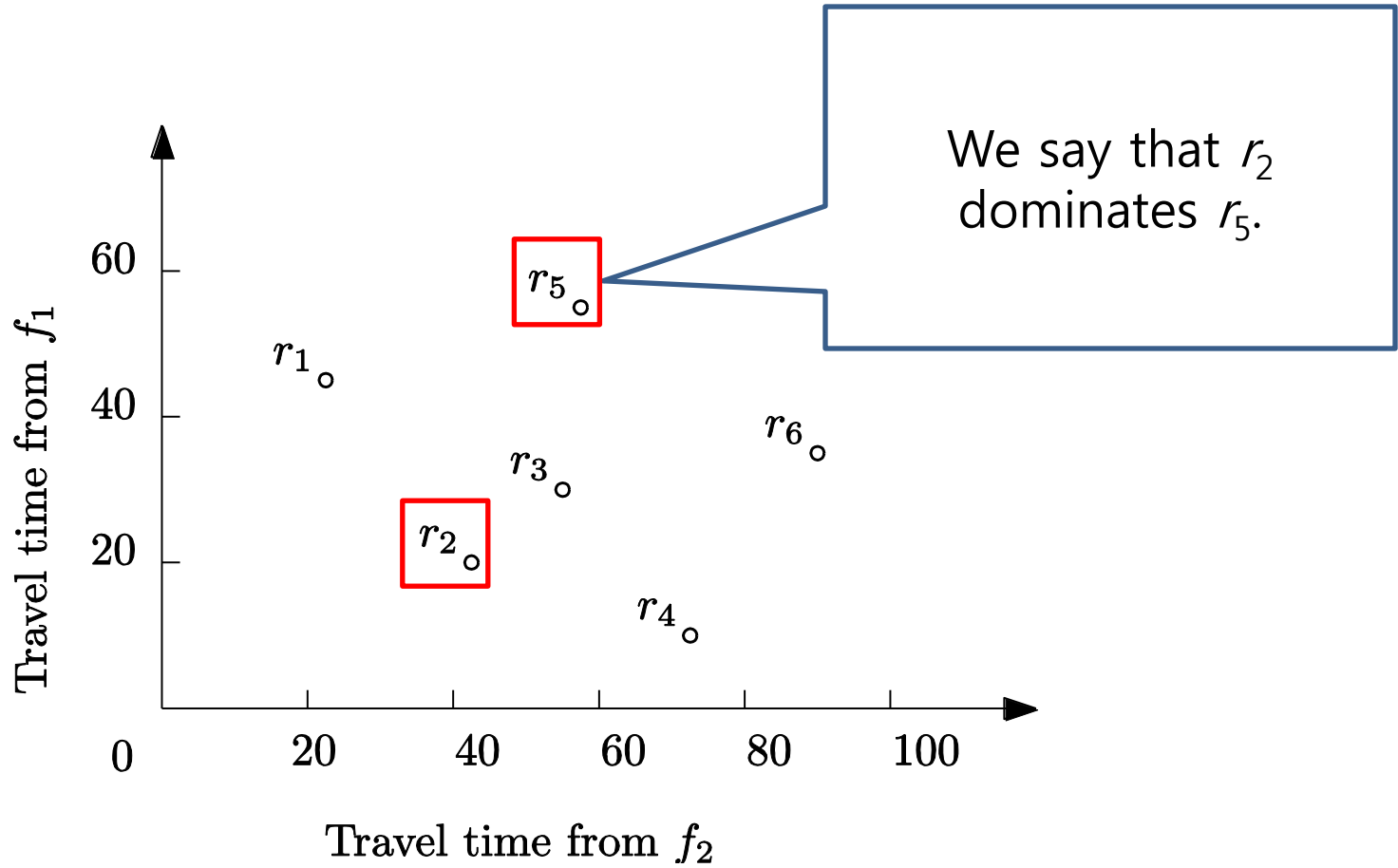
Introduction



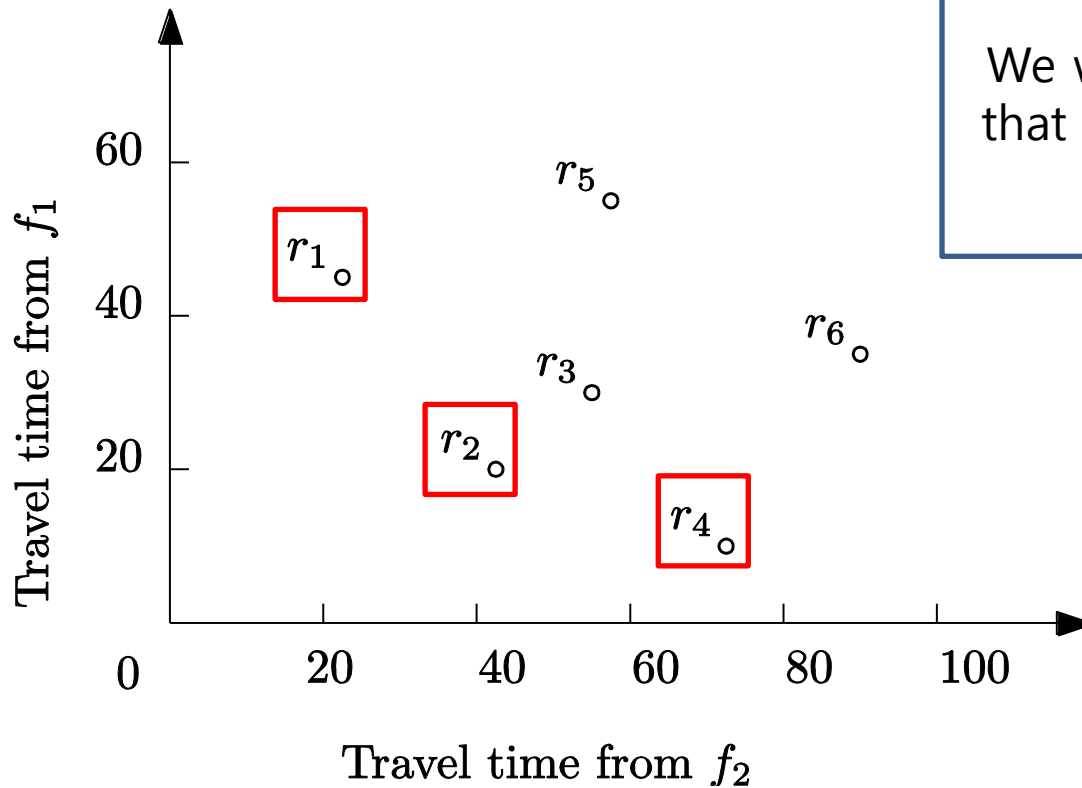
Introduction



Introduction

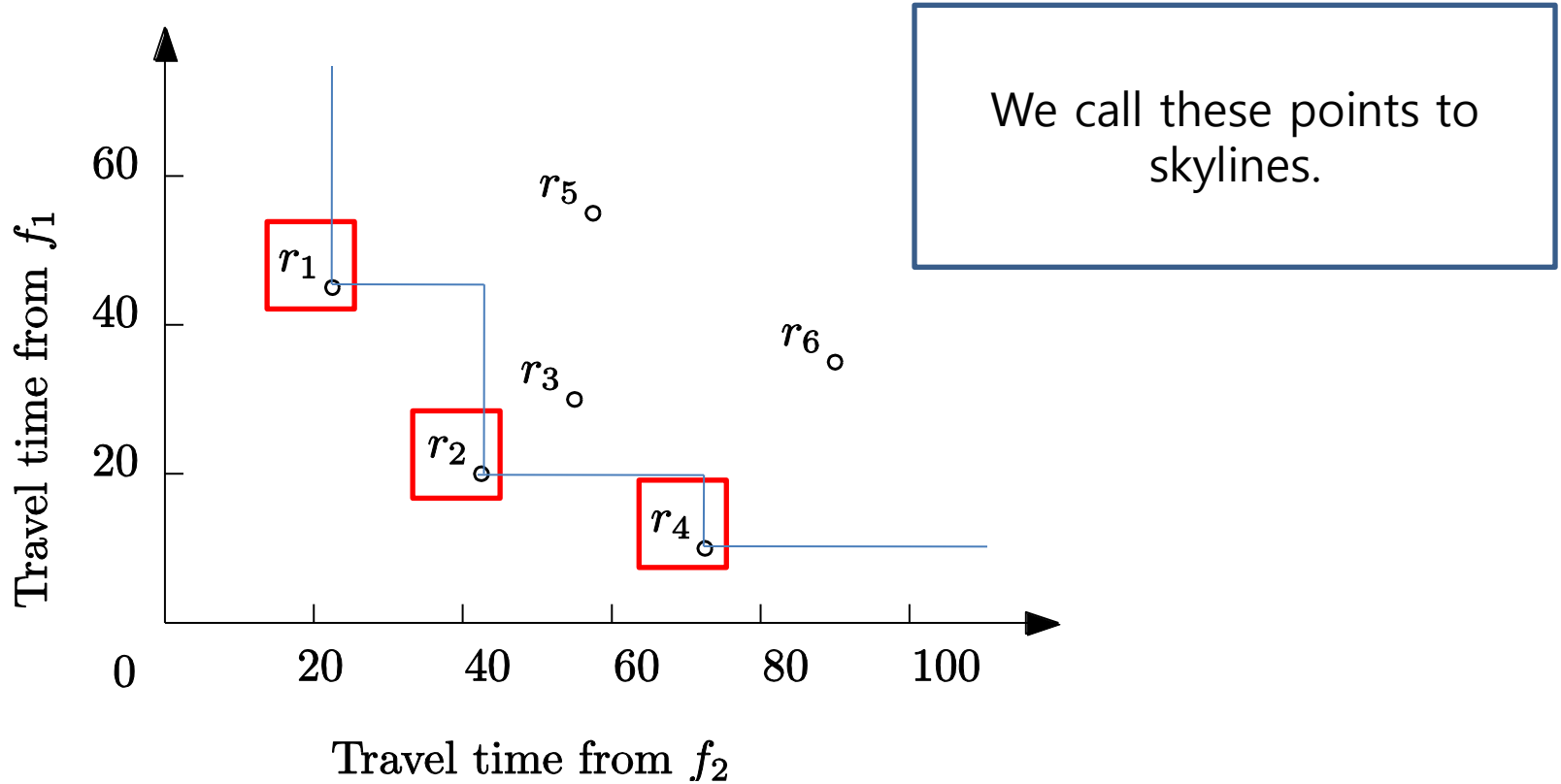


Skyline



We want to find all points that are not dominated by any other point.

Skyline



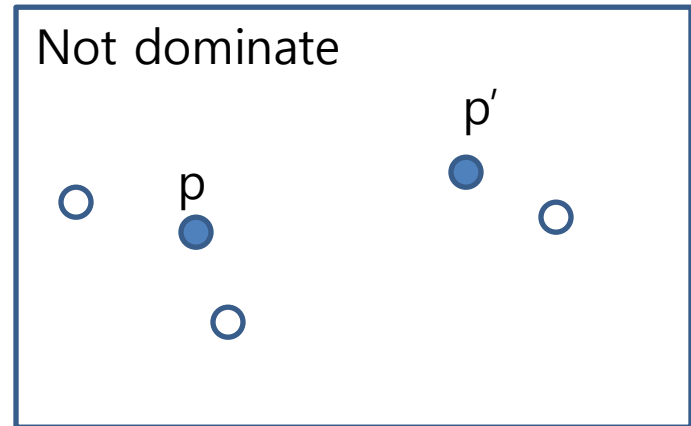
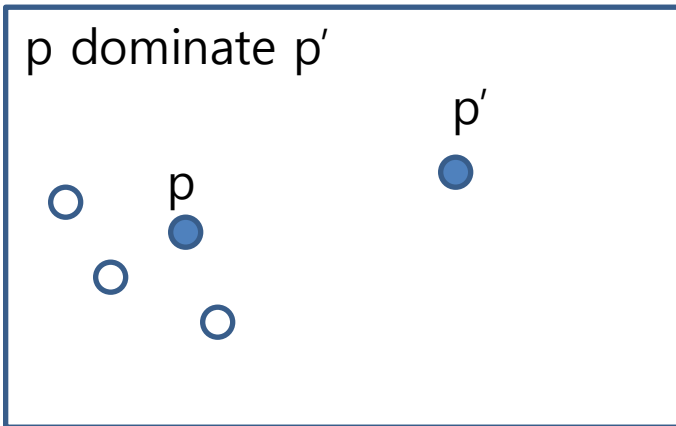
Problem Definition

In the plane

- Input
 - P : the set of data points
 - Q : the set of query points ($|P| \geq |Q|$)
- output
 - S : the skyline ($S \subseteq P$)

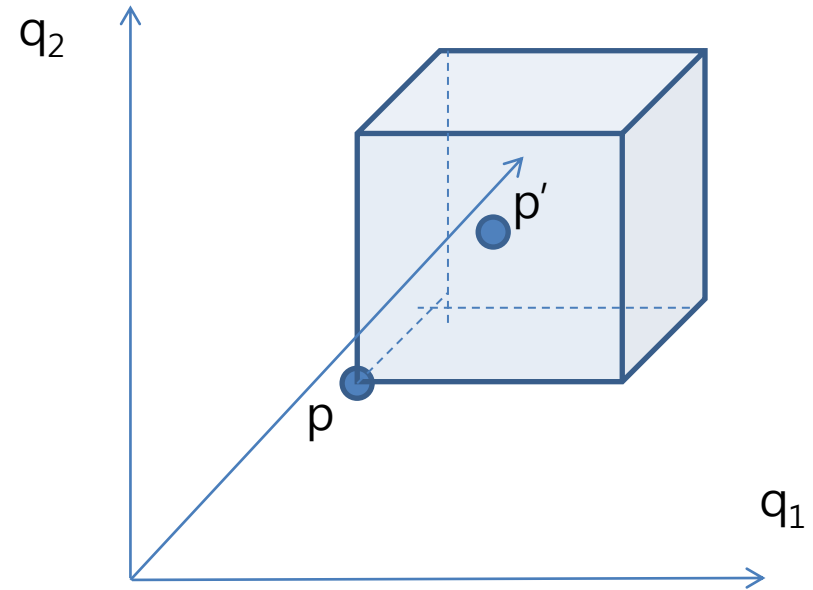
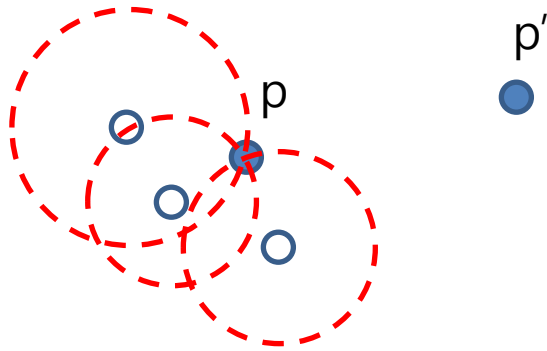
We want to compute the set S of all spatial skyline points from P with respect to Q in the plane

Problem Definition



Problem Definition

p dominate p'



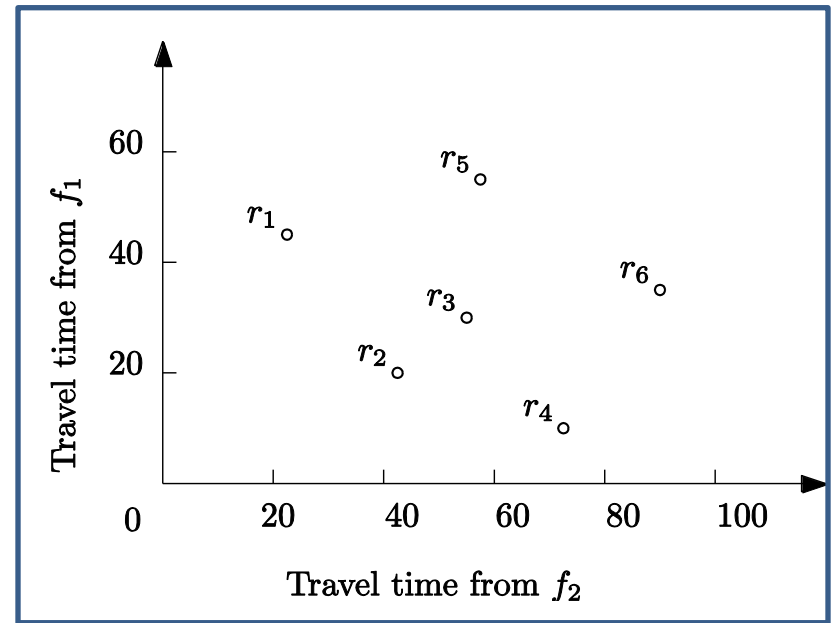
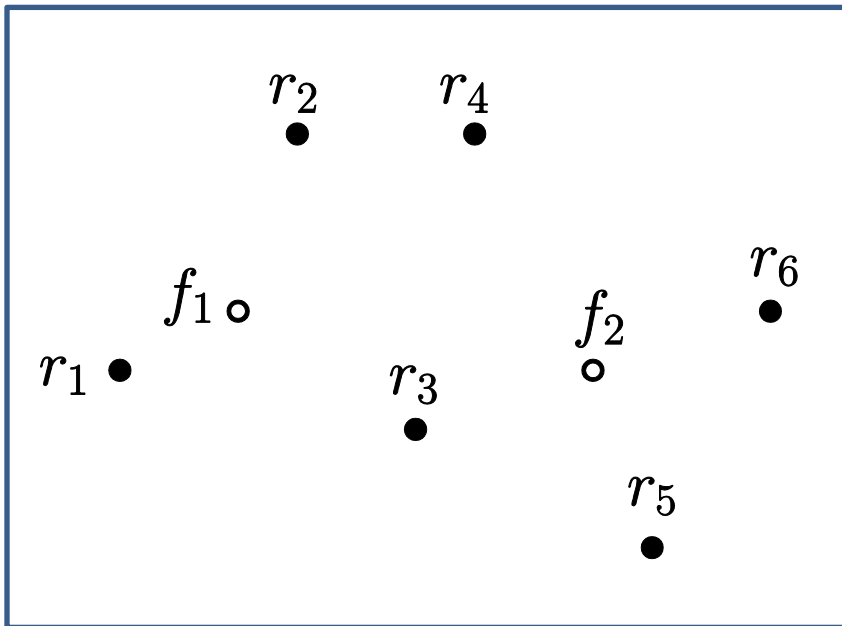
- **Definition : dominate**

We say that p_1 dominates p_2 if and only if $d(p_1, q) \leq d(p_2, q)$ for every $q \in Q$ and $d(p_1, q') < d(p_2, q')$ for some $q' \in Q$.

Problem Definition

$$P = \{r_1, r_2, r_3, r_4, r_5\}$$

$$Q = \{f_1, f_2\}$$

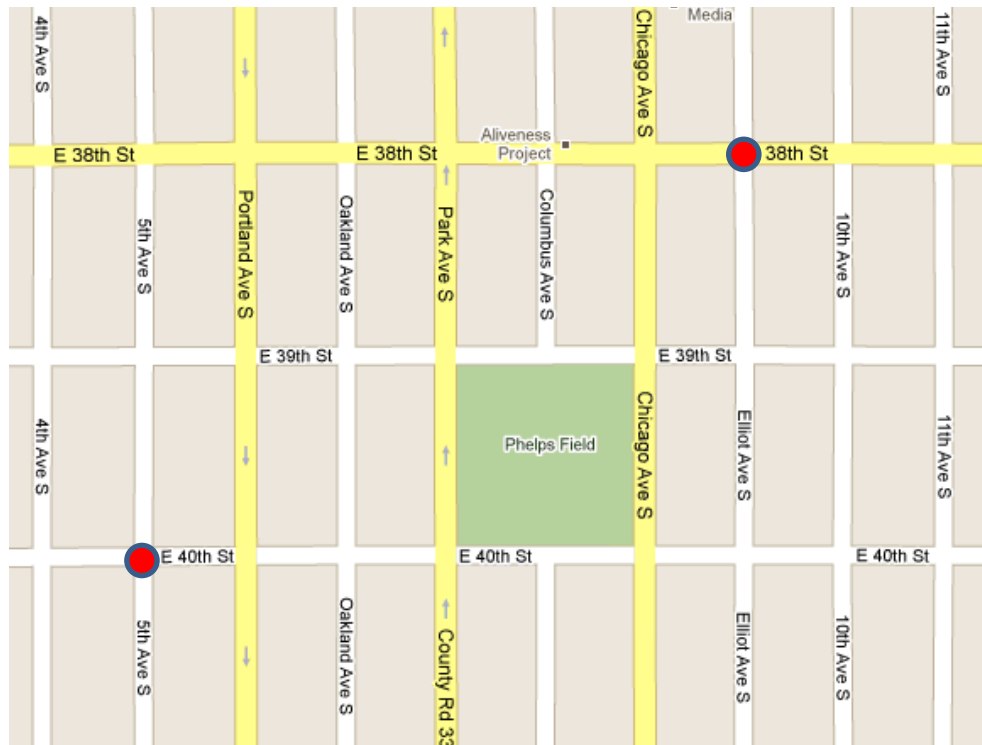


L_1 metric

- L_1 distance between two points (x_1, y_1) and (x_2, y_2) in the plane is $|x_1 - x_2| + |y_1 - y_2|$.
- L_1 metric is reasonable to represent a well-developed road network.

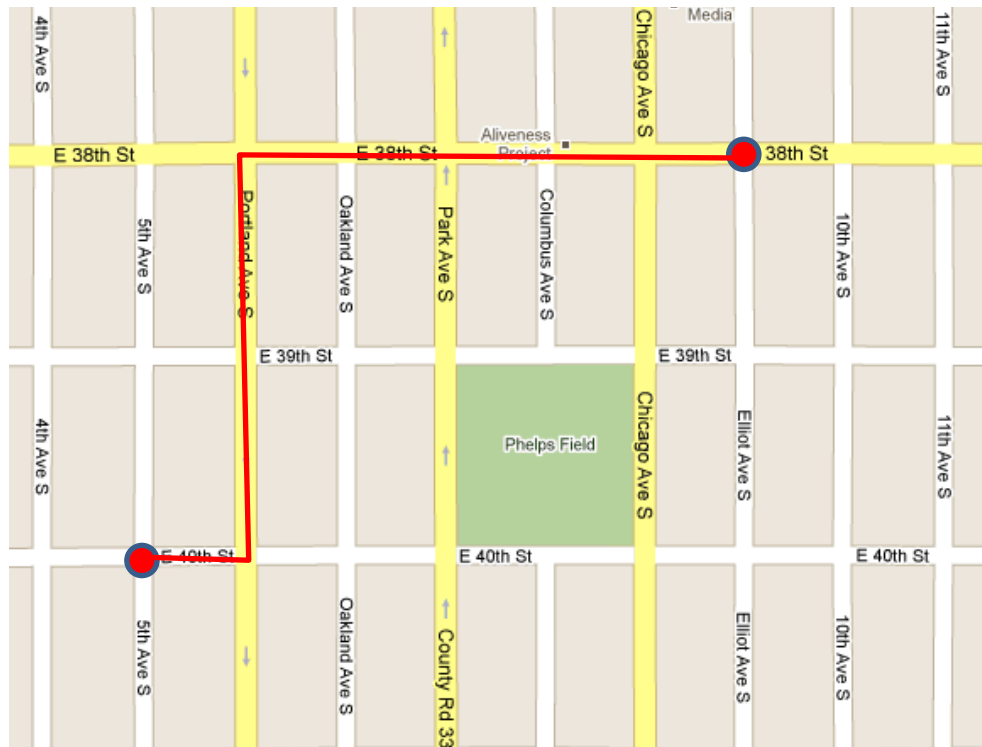
L_1 metric

- L_1 metric is reasonable to represent a well-developed road network.



L_1 metric

- L_1 metric is reasonable to represent a well-developed road network.

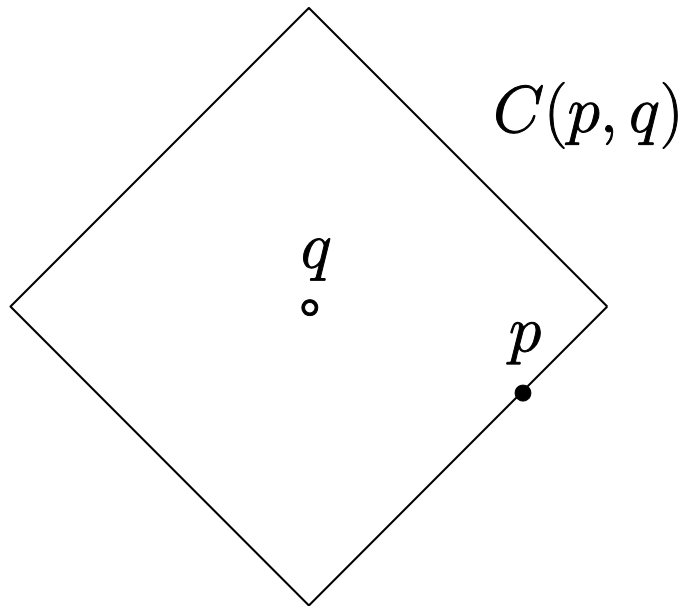


Related work

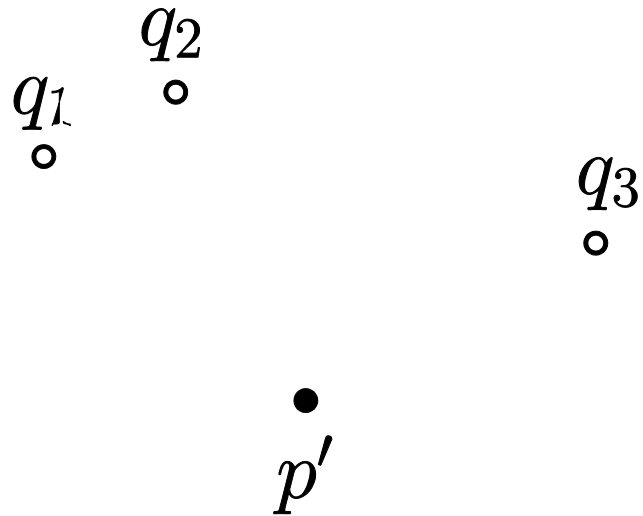
- Spatial skyline queries for the other metrics.
 - Based on pairwise dominance test
- Skyline queries
 - Based on pairwise dominance test
 - Operations for d dimensional data

L_1 metric

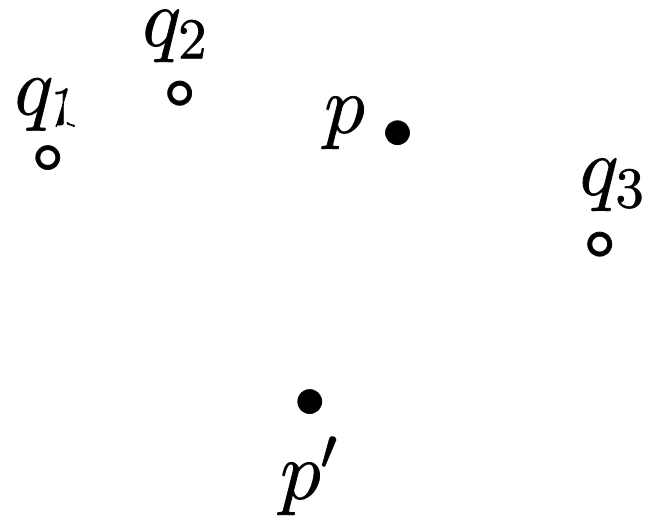
In the plane, we use L_1 metric for the distance between two points.



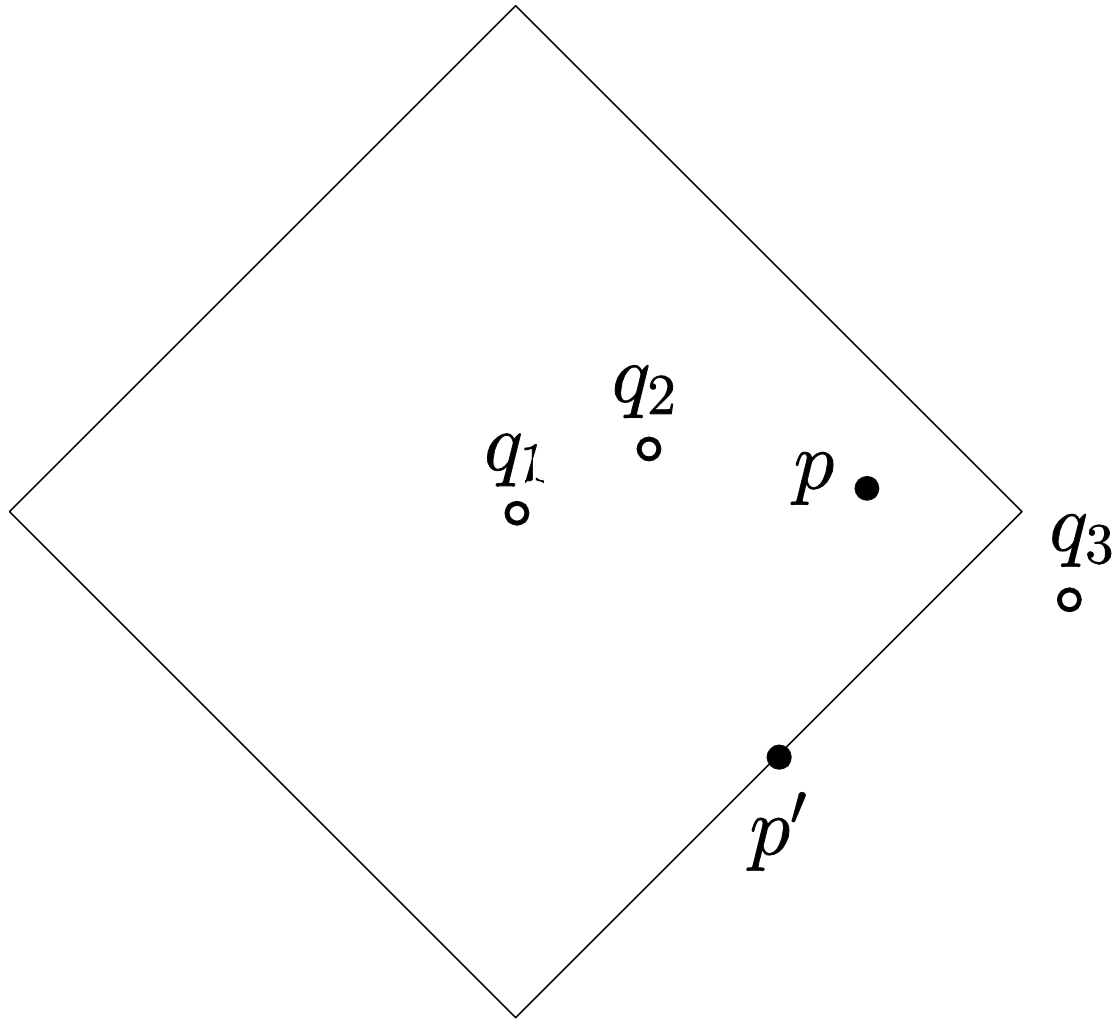
Observation



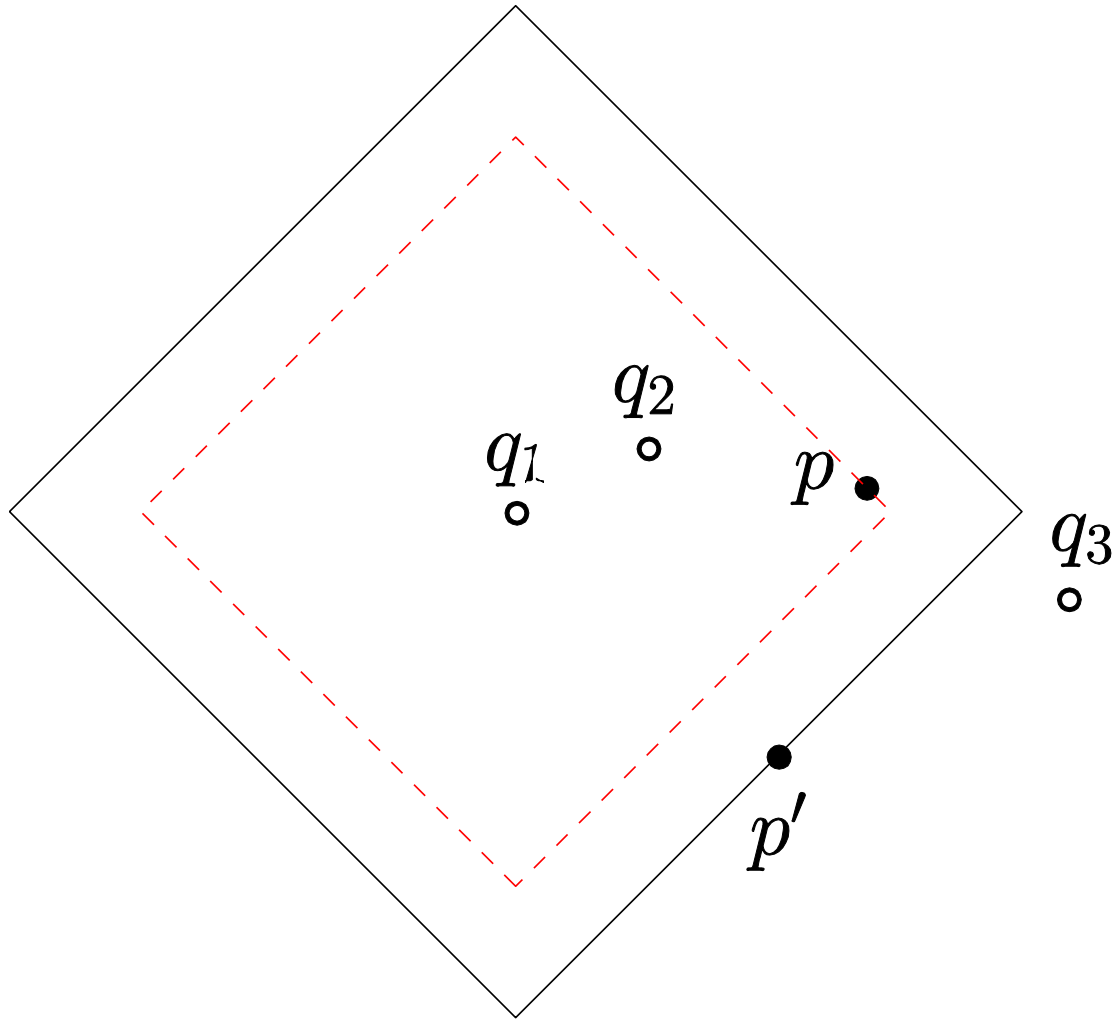
Observation



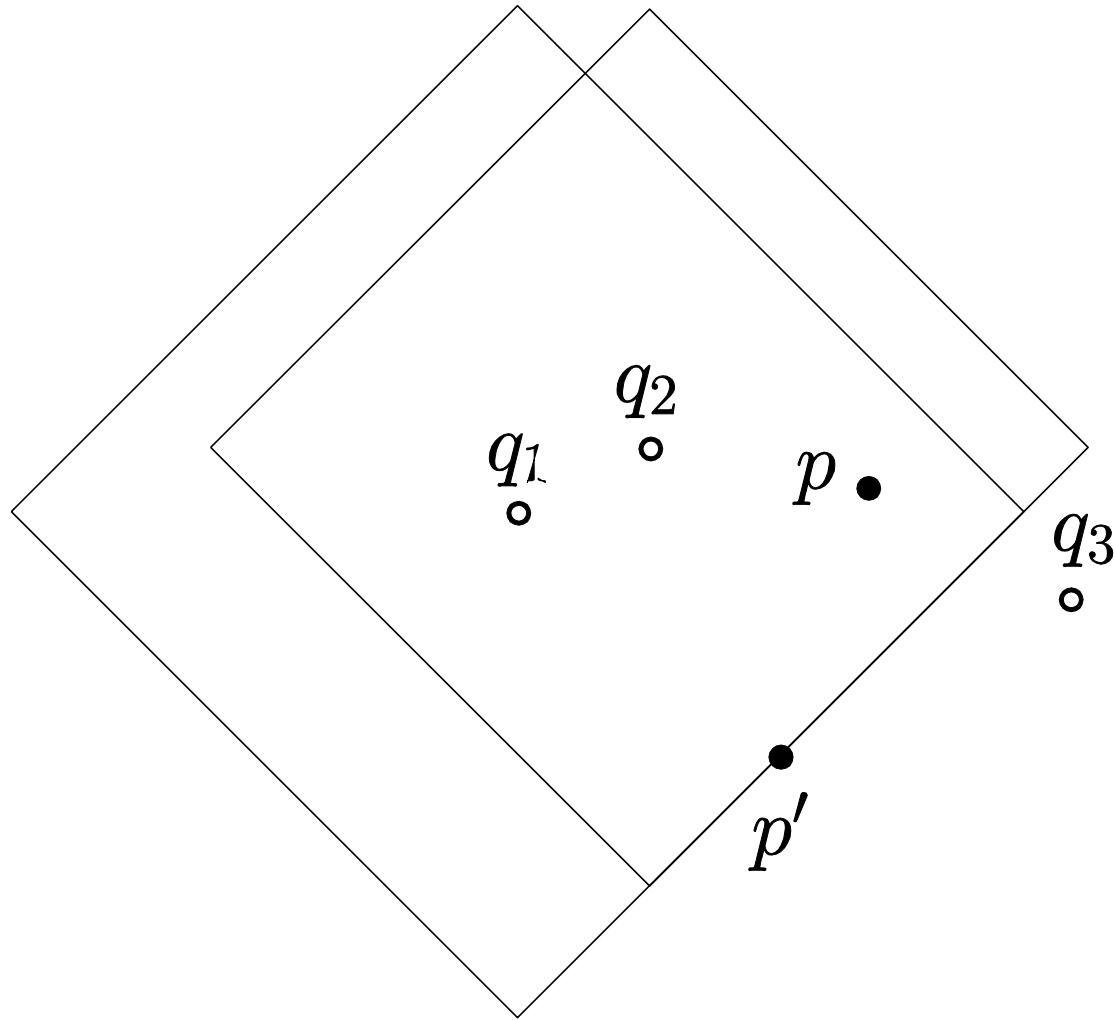
Observation



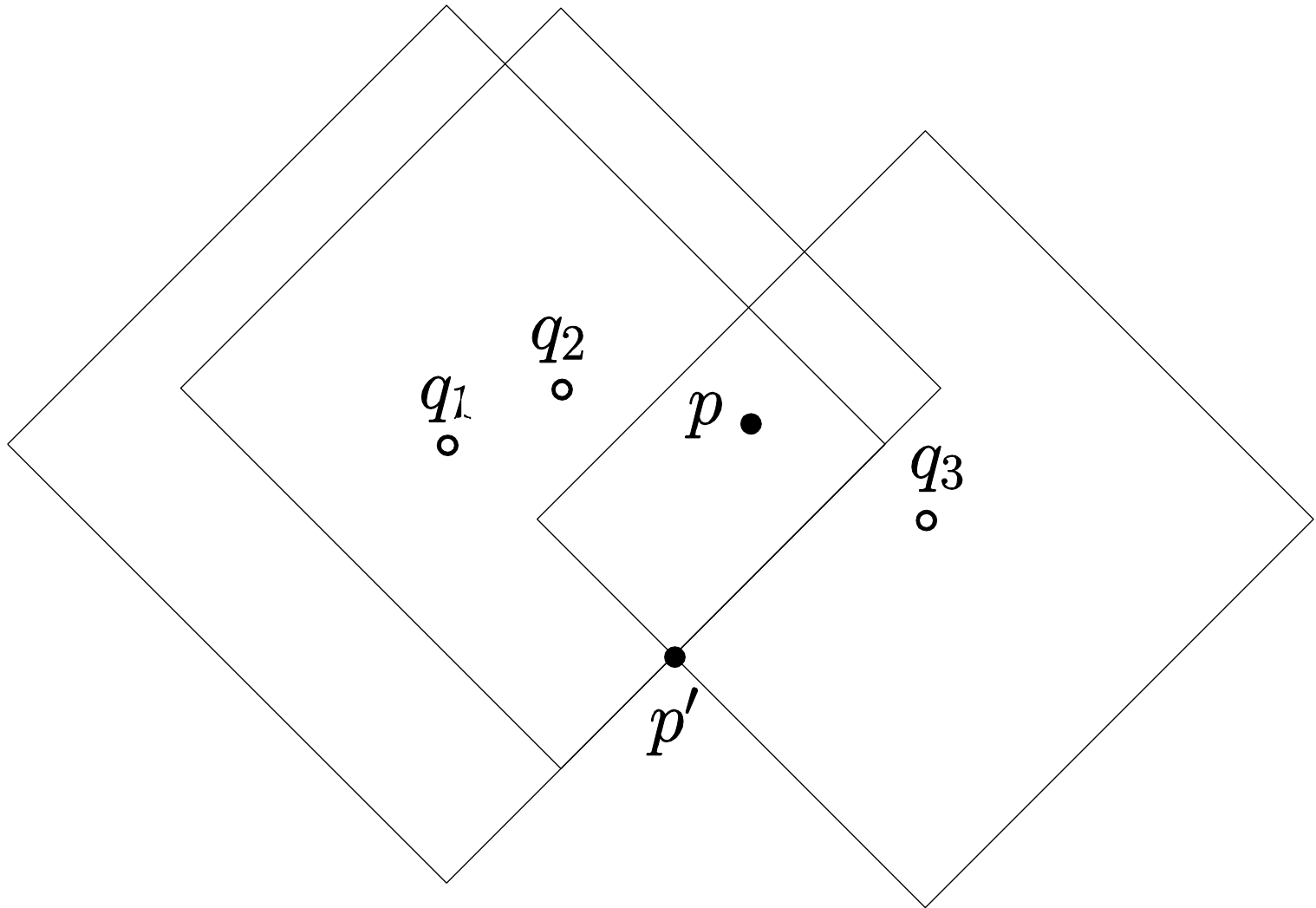
Observation



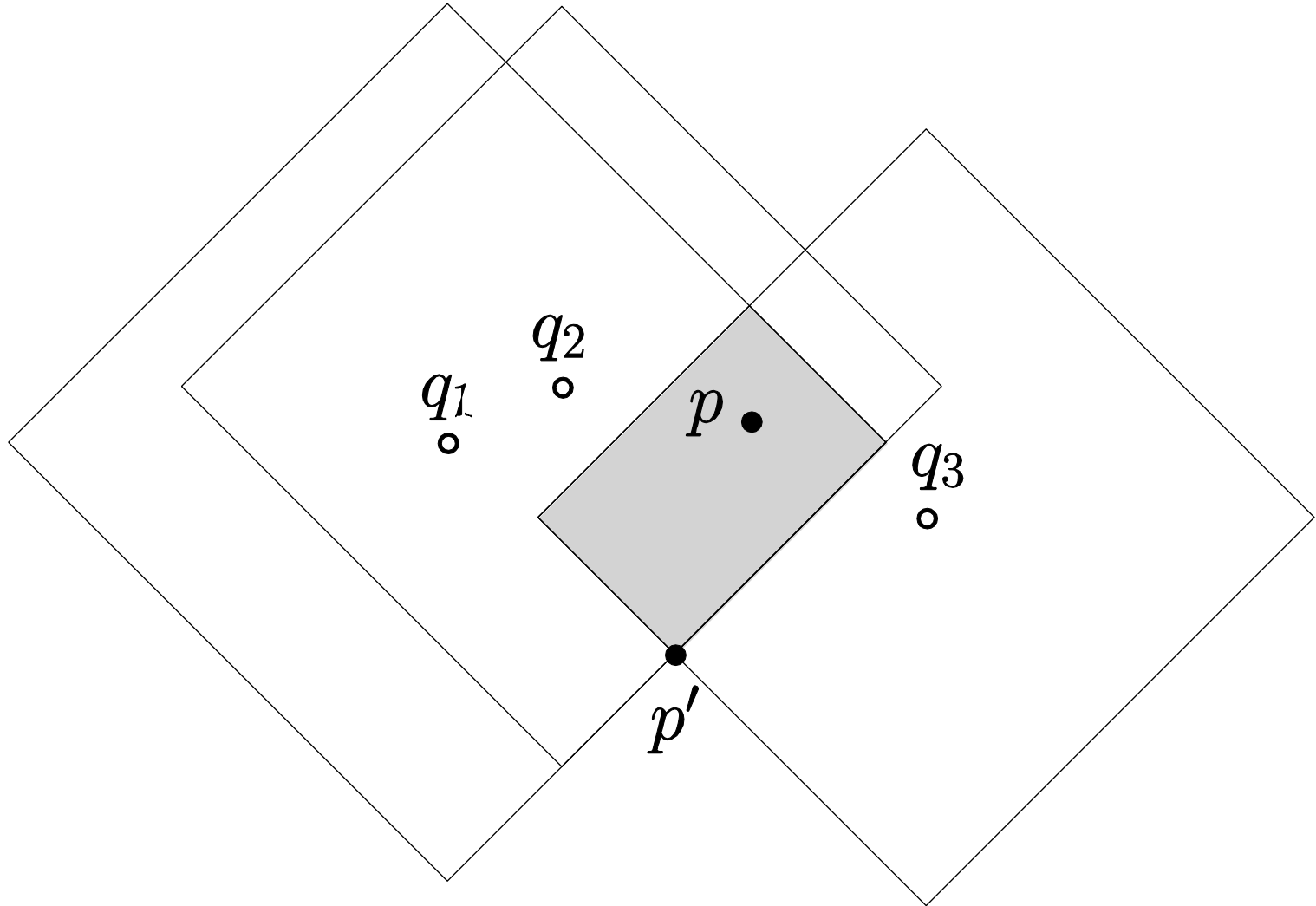
Observation



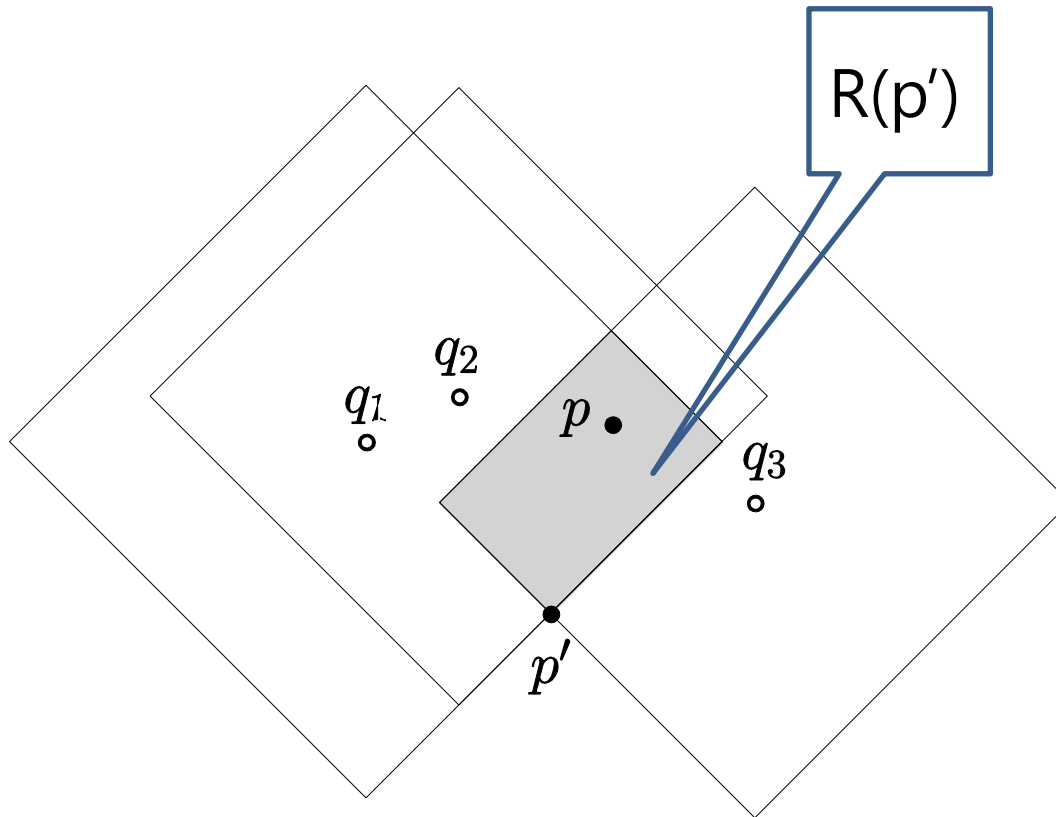
Observation



Observation



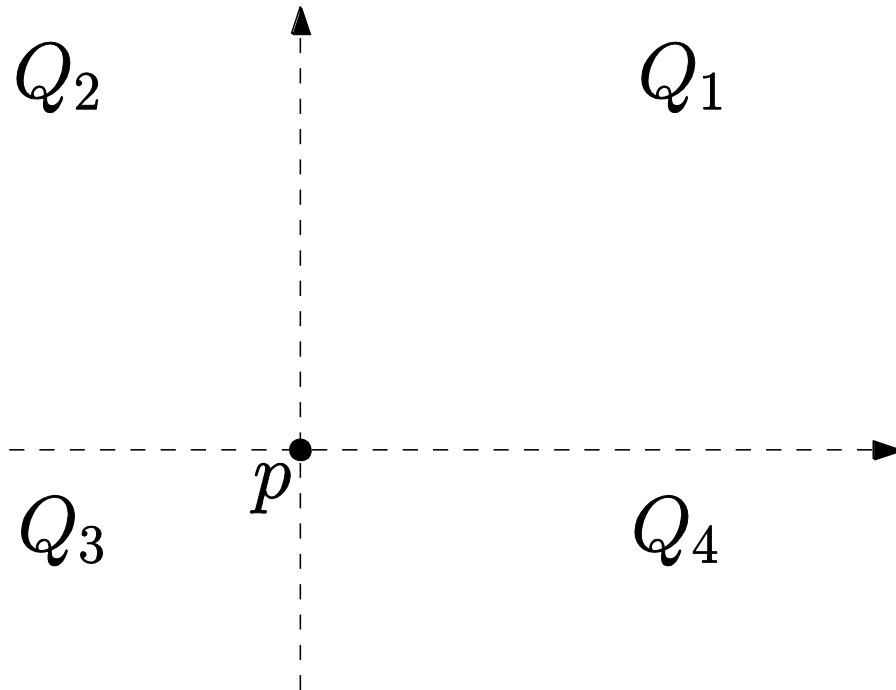
Observation



Computing $R(p')$ takes $O(|Q|)$ time for each point in P

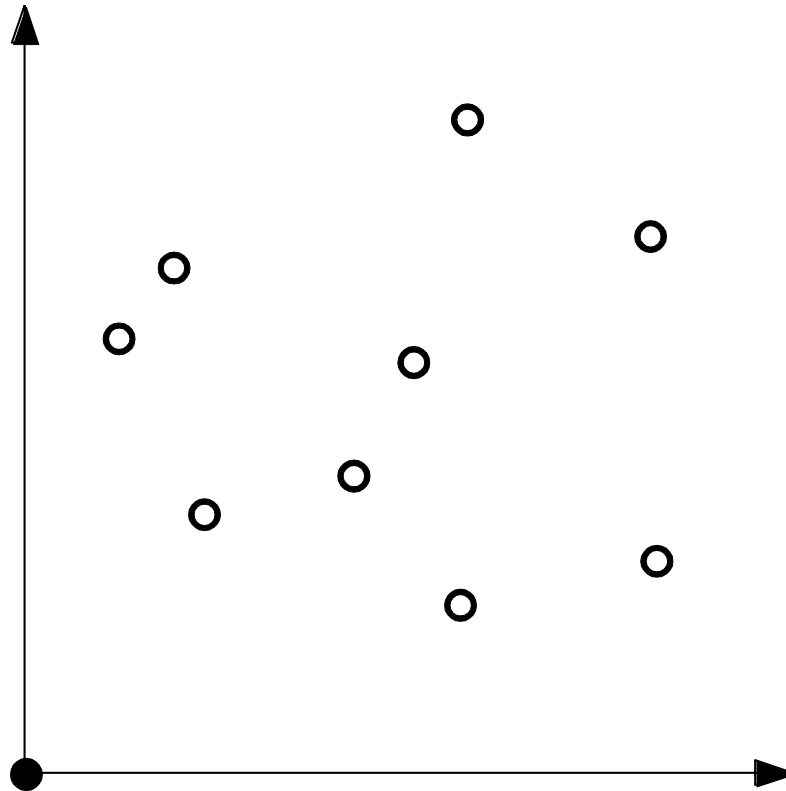
Computing $R(p)$

- There are at most four query points that determine the $R(p)$

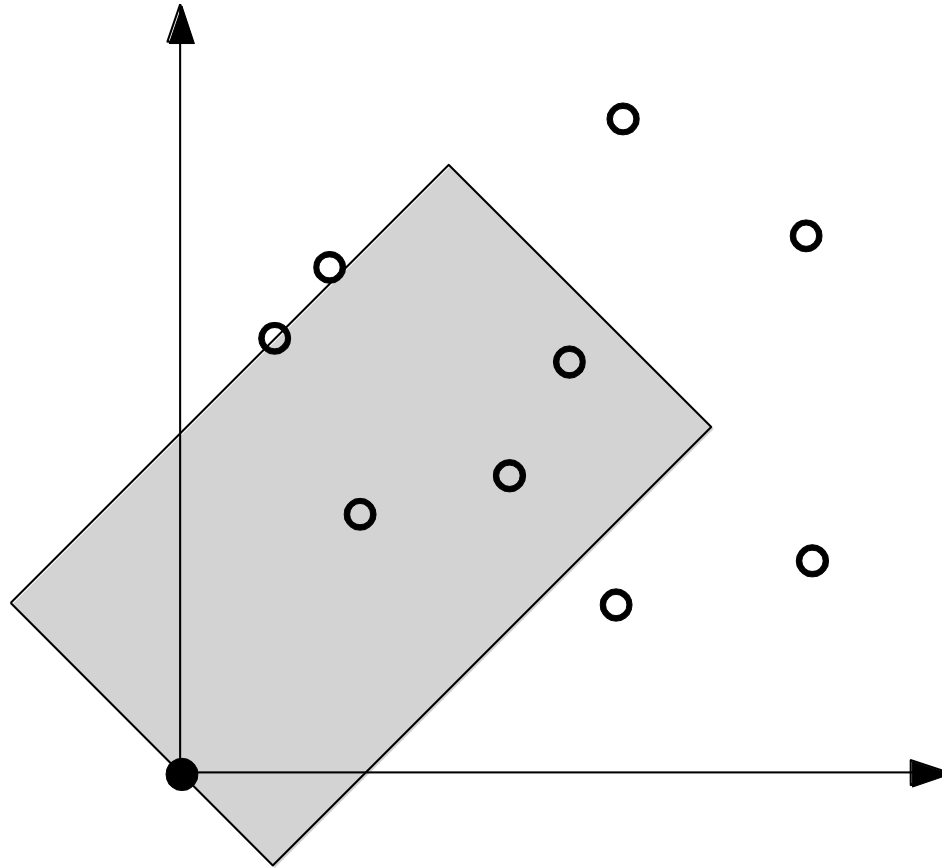


Computing $R(p)$

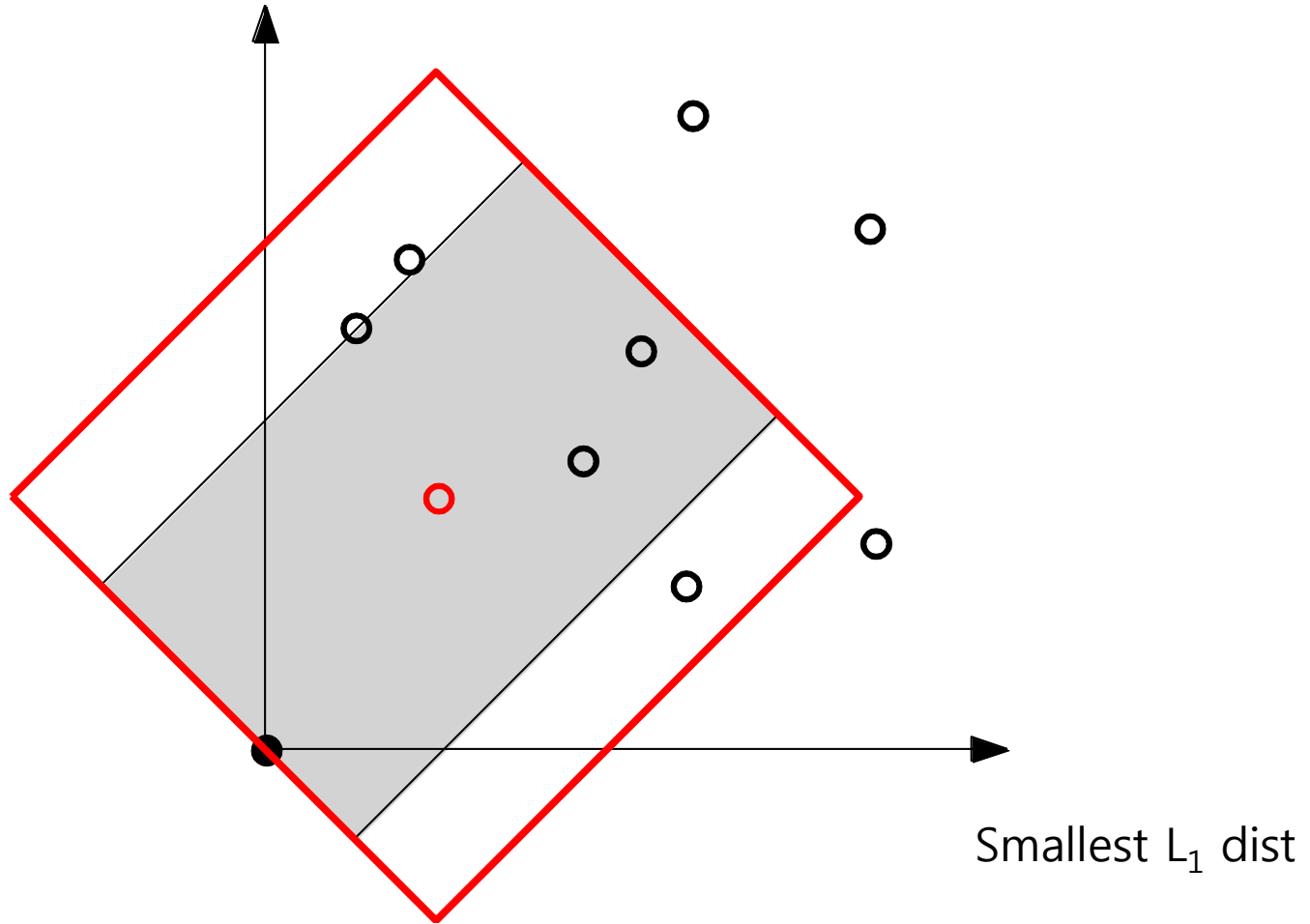
$$Q_1 = Q$$



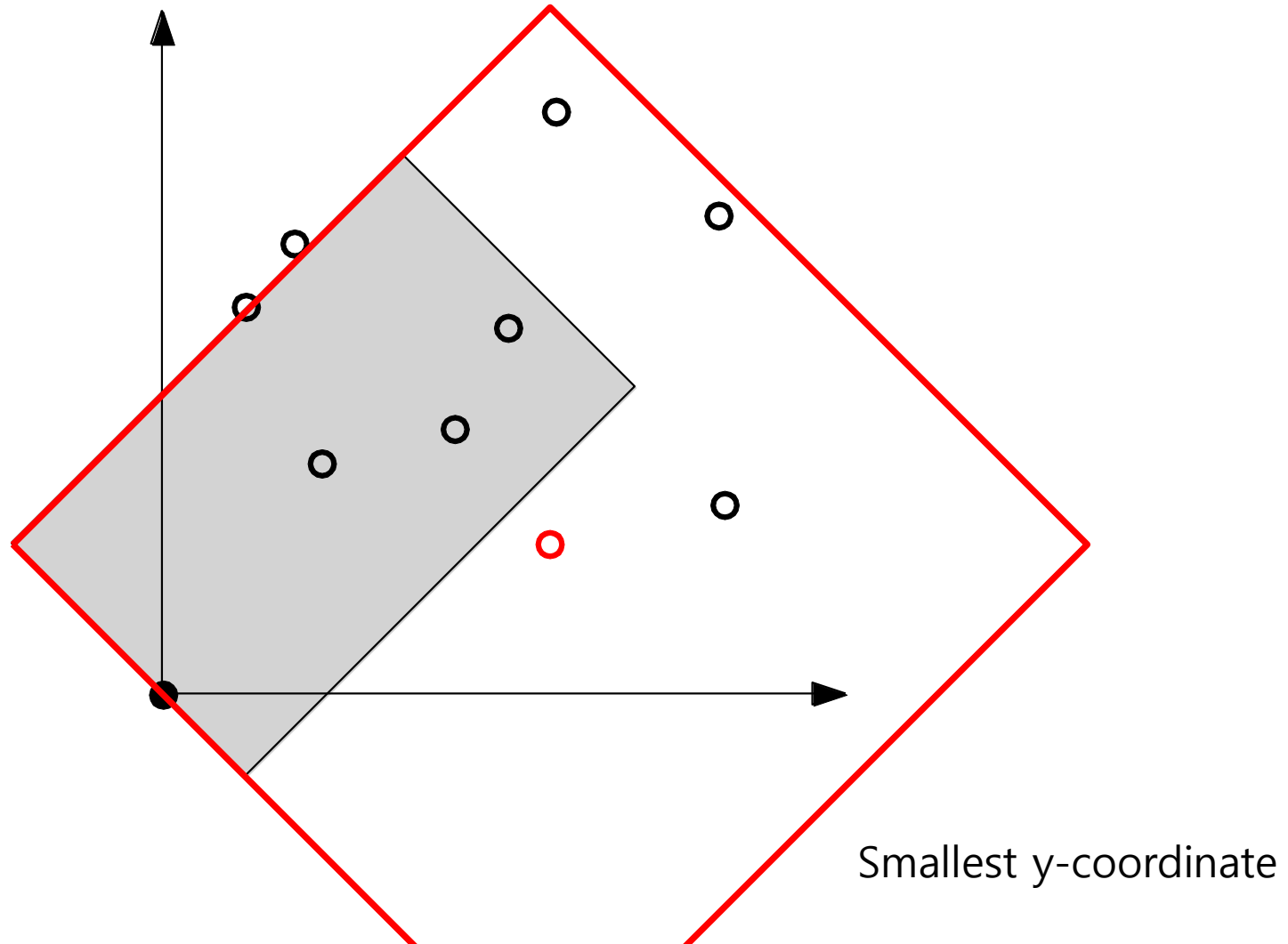
Computing $R(p)$

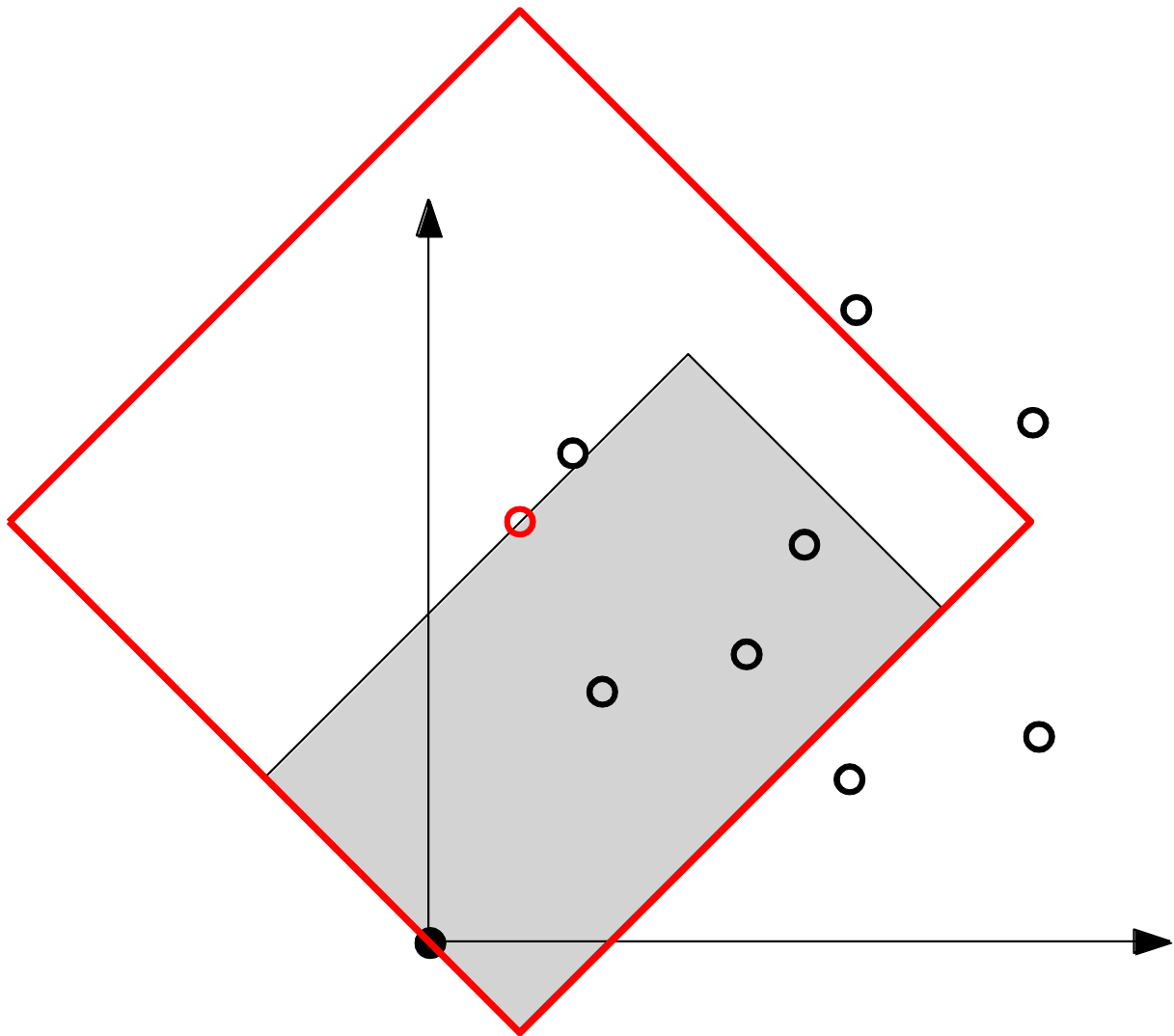


Computing $R(p)$



Computing $R(p)$

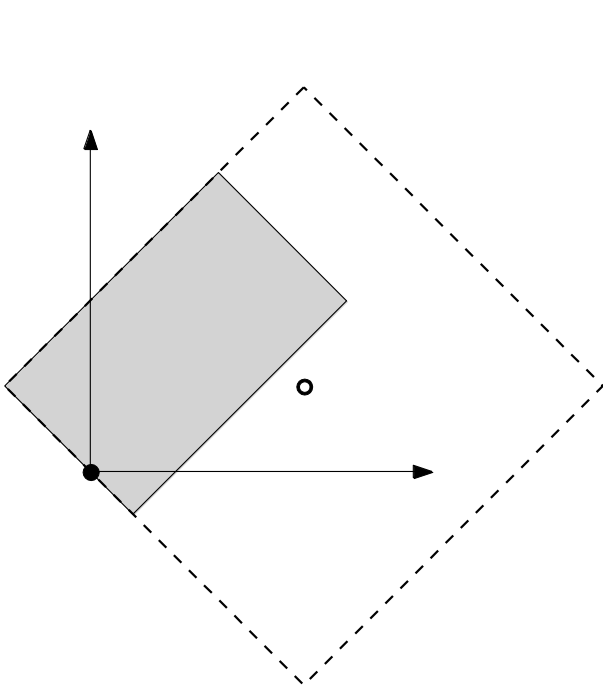




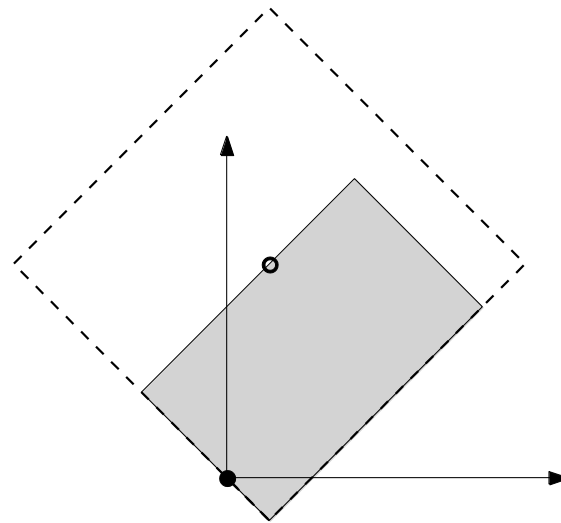
Smallest x-coordinate

Computing $R(p)$

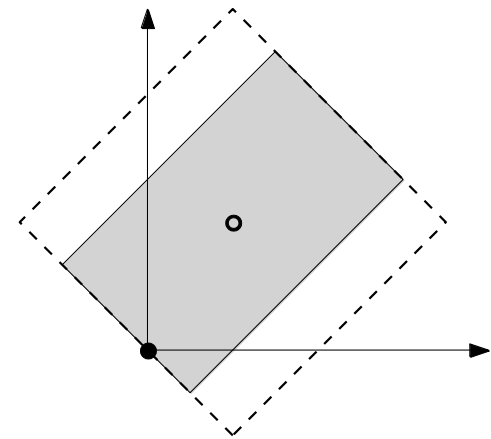
The case that $Q_1=Q$



Smallest y-coordinate

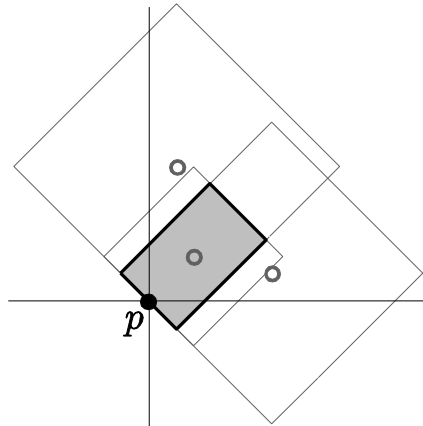


Smallest x-coordinate

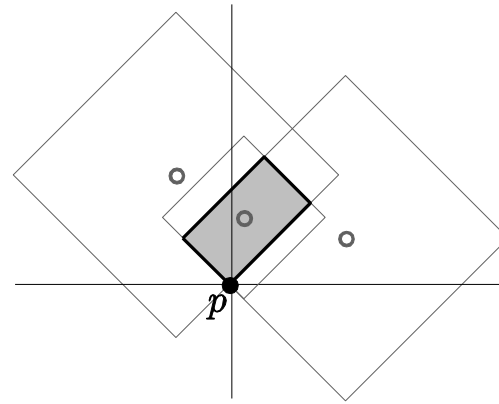


Smallest L_1 dist

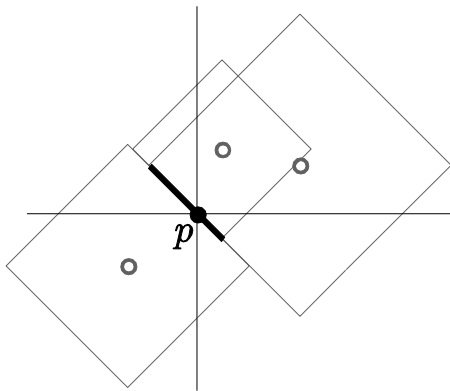
Computing $R(p)$



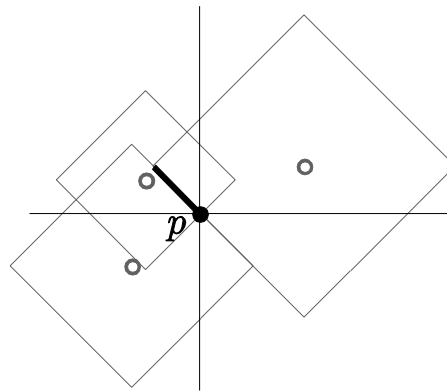
$$Q_1 = Q$$



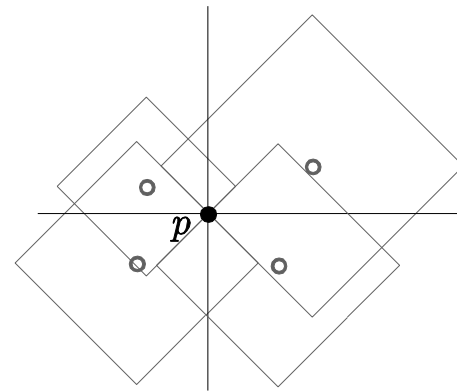
$$Q_1 \cup Q_2 = Q$$



$$Q_1 \cup Q_3 = Q$$



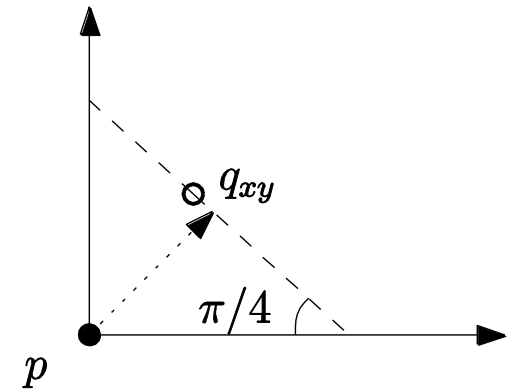
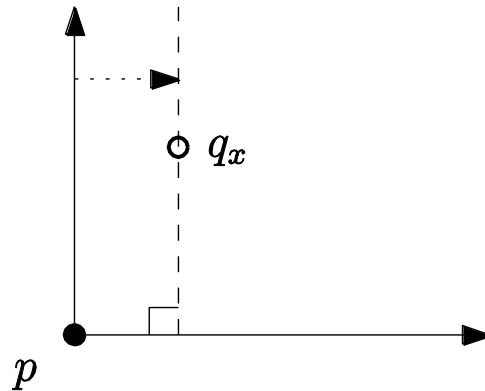
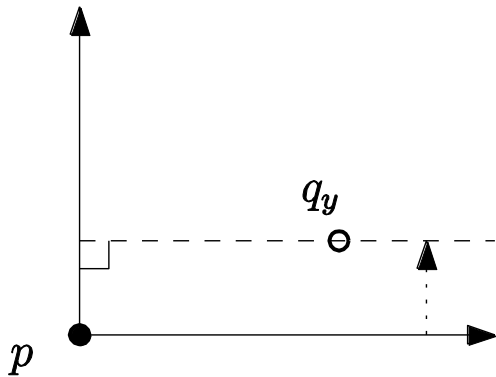
$$Q_1 \cup Q_2 \cup Q_3 = Q$$



$$Q_1 \cup Q_2 \cup Q_3 \cup Q_4 = Q$$

Computing $R(p)$

Using segment dragging queries



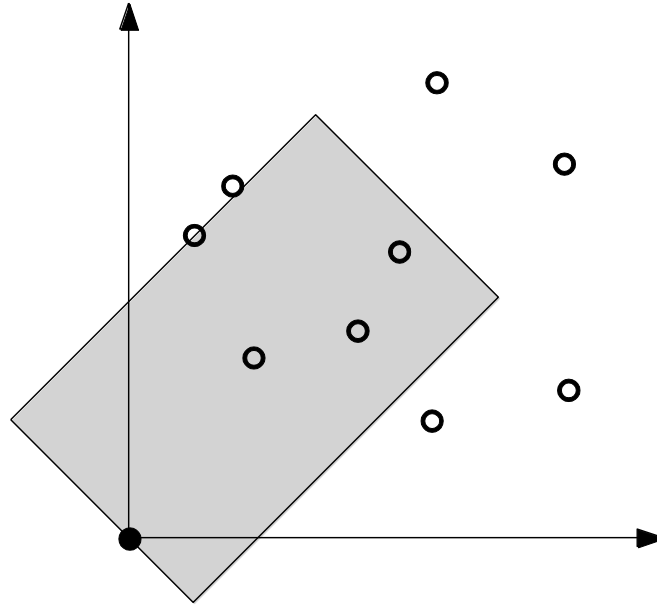
$O(n \log n)$ time preprocessing

$O(\log n)$ time for each query

$O(n)$ space

Range counting query

- Using range counting query to count the number of data points in $R(p)$



Three cases for $R(p)$

- Three cases for data points contained in $R(p)$

Three cases for $R(p)$

- Three cases for data points contained in $R(p)$
 - (a) no data point in $R(p)$, other than p
 - p is skyline

Three cases for $R(p)$

- Three cases for data points contained in $R(p)$
 - (a) no data point in $R(p)$, other than p
 - (b) some data point p' in the interior of $R(p)$

→ p is not skyline

Three cases for $R(p)$

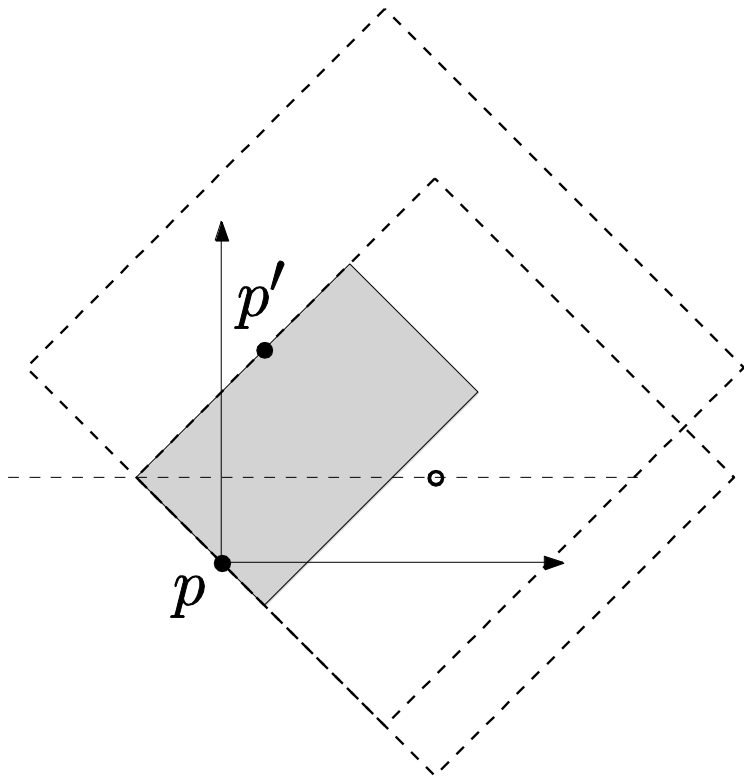
- Three cases for data points contained in $R(p)$
 - (a) no data point in $R(p)$, other than p
 - (b) some data point p' in the interior of $R(p)$
 - (c) some data point p' in $R(p)$, but no data point in the interior of $R(p)$

Three cases for $R(p)$

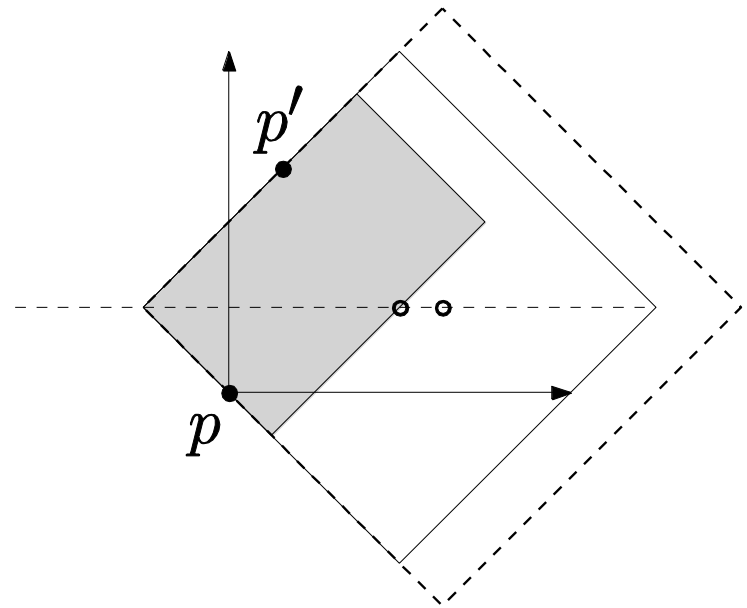
- Three cases for data points contained in $R(p)$
 - (a) no data point in $R(p)$, other than p
 - (b) some data point p' in the interior of $R(p)$
 - (c) some data point p' in $R(p)$, but no data point in the interior of $R(p)$
- **Definition : dominate**

We say that p_1 dominates p_2 if and only if $d(p_1, q) \leq d(p_2, q)$ for every $q \in Q$ and $d(p_1, q') < d(p_2, q')$ for some $q' \in Q$.

Case (c)



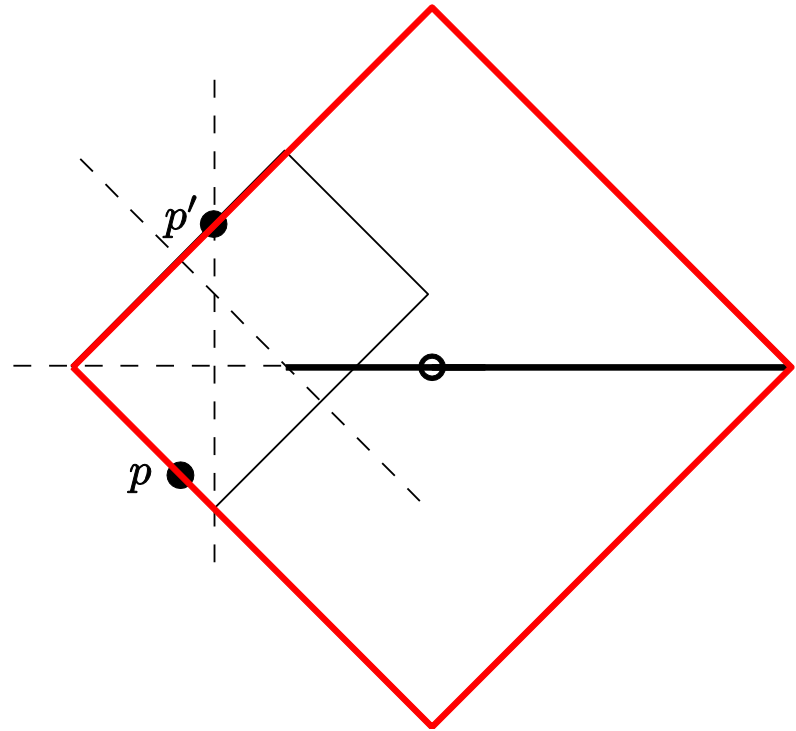
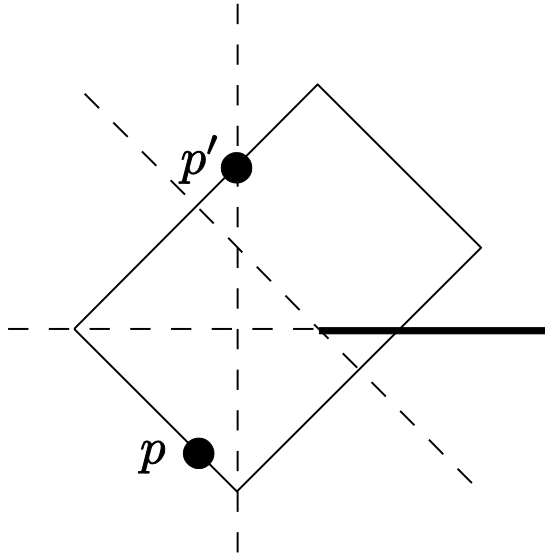
p' dominates p



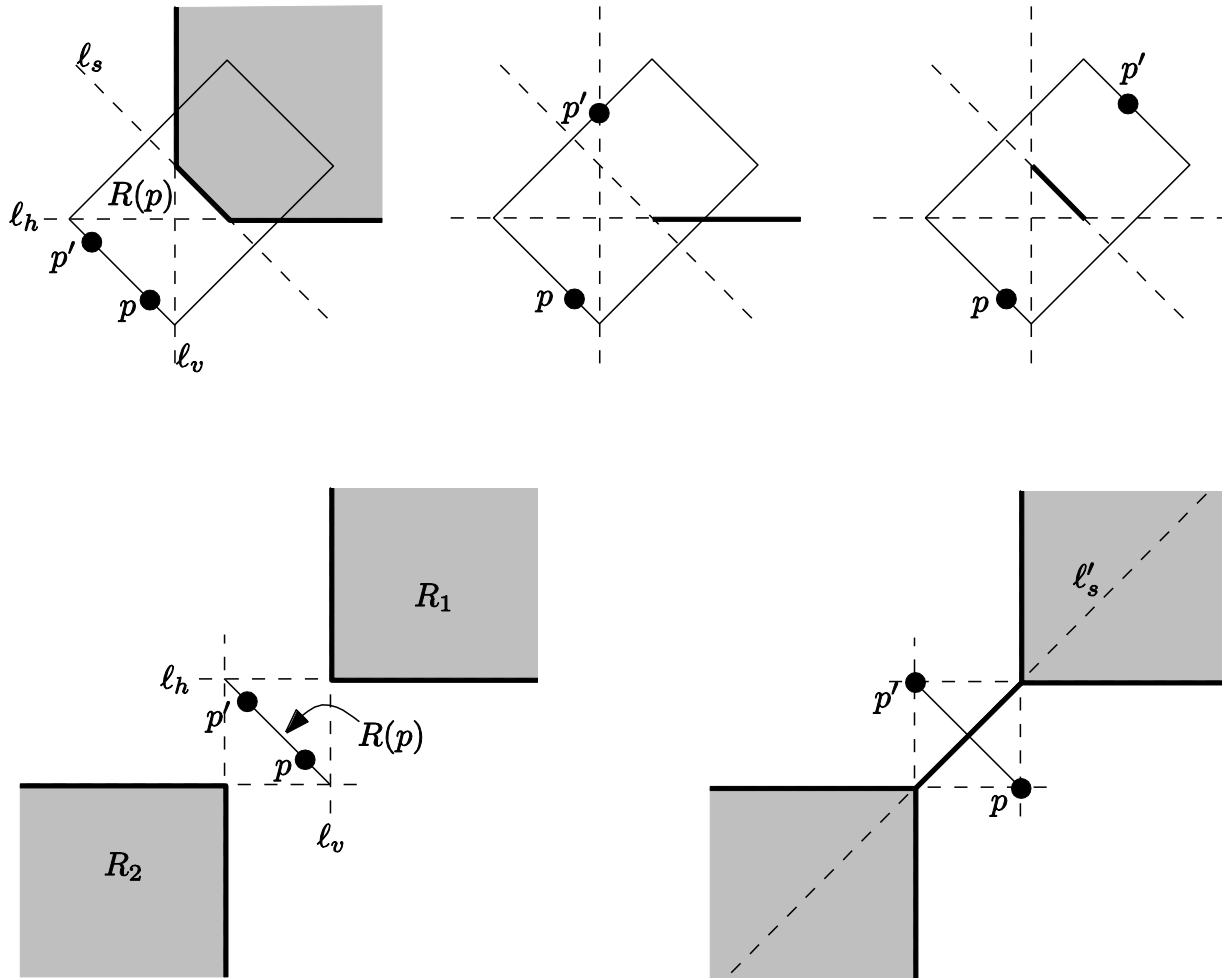
p' does not dominate p

Case (c)

The case that $Q_1=Q$



Case (c)

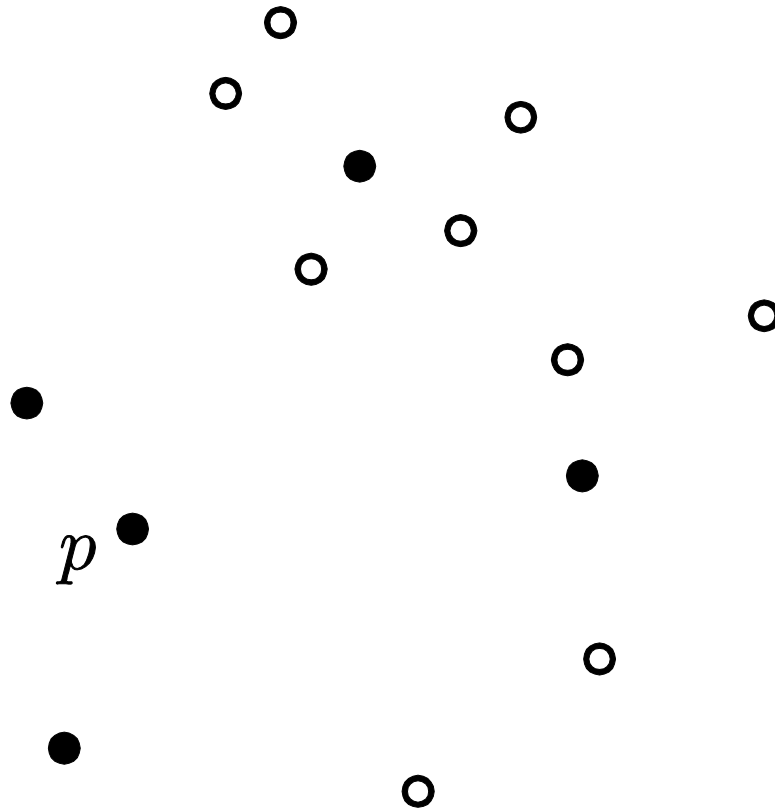


Algorithm

- **Input: P,Q**
 - **Output: S**
1. Compute
 - a range counting query structure of P
 - a segment dragging query structure of Q

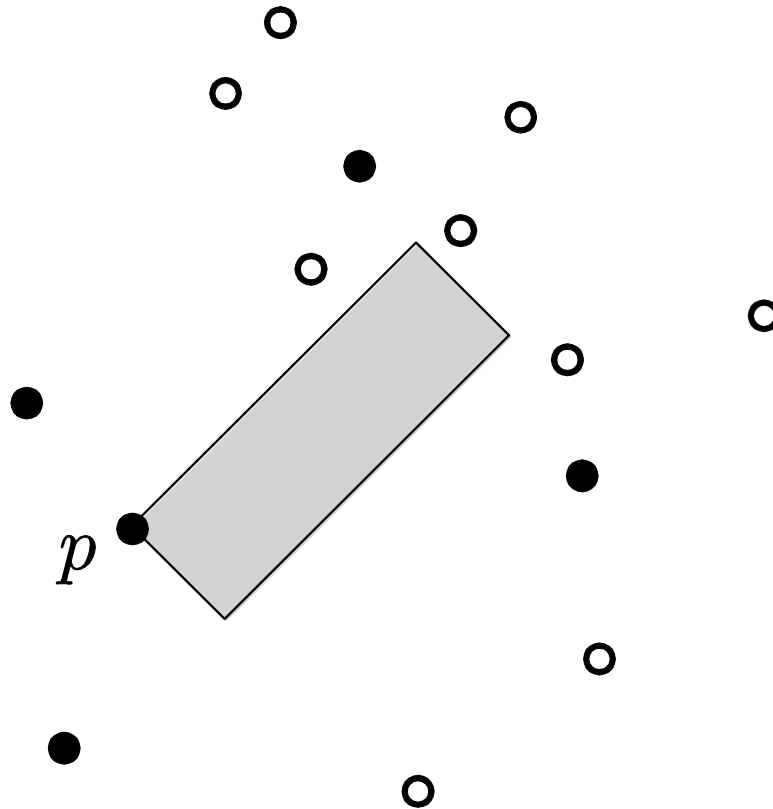
Algorithm

2. For each point p , compute $R(p)$



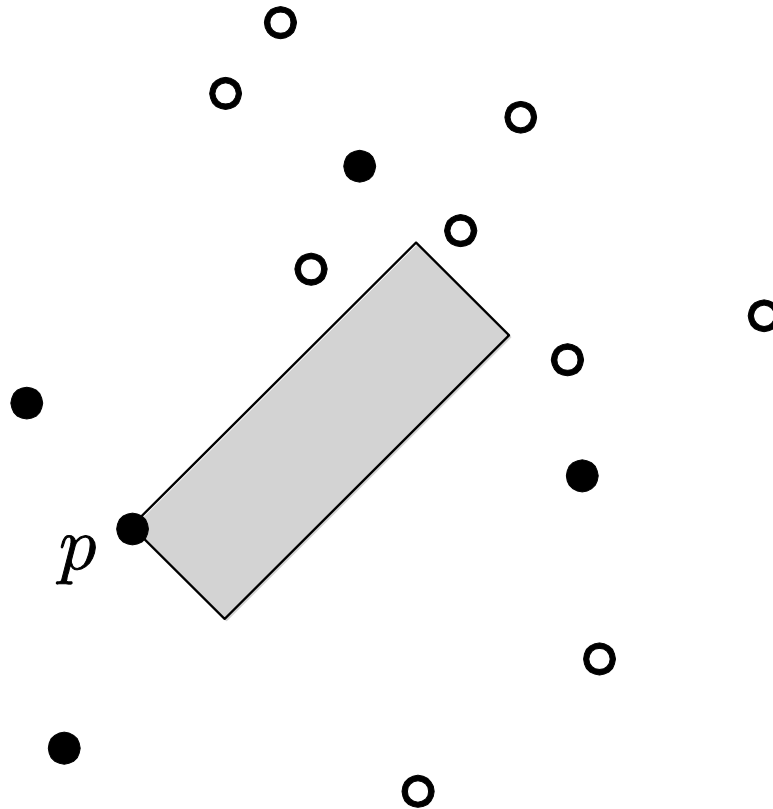
Algorithm

2. For each point p , compute $R(p)$



Algorithm

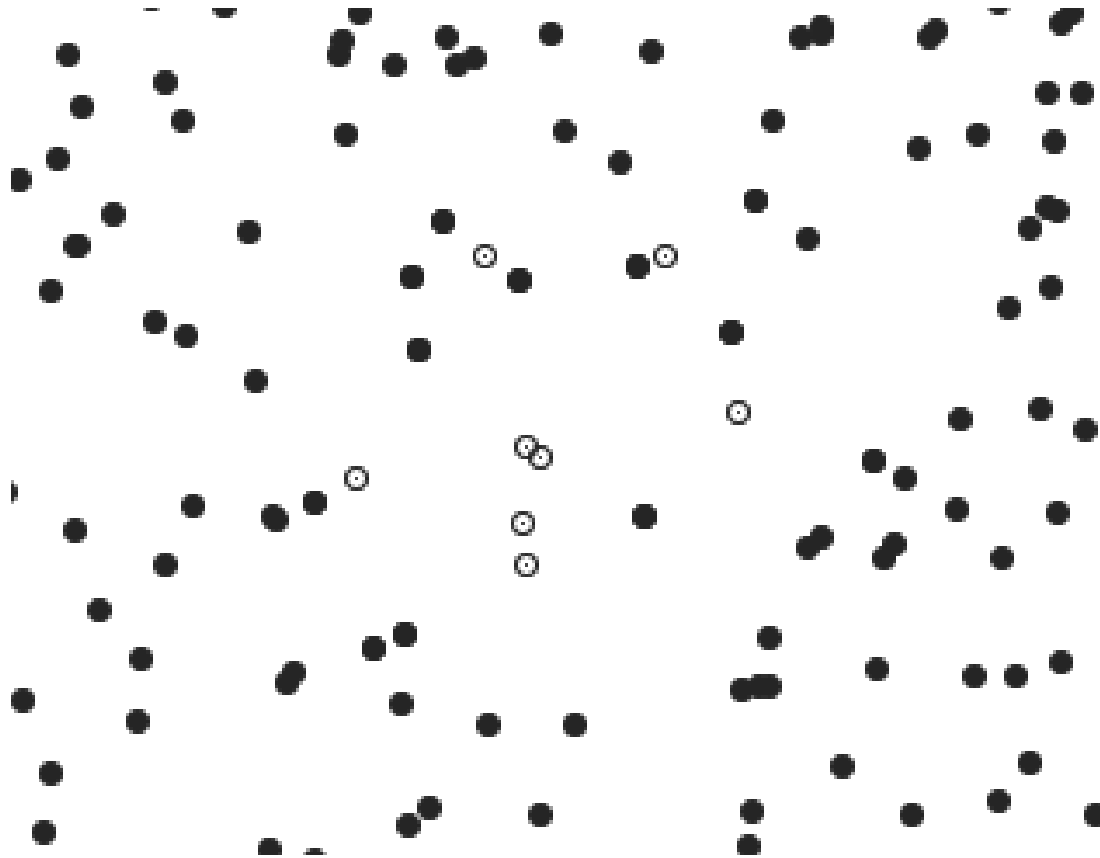
3. test whether p is skyline or not by the Range counting query for $R(p)$



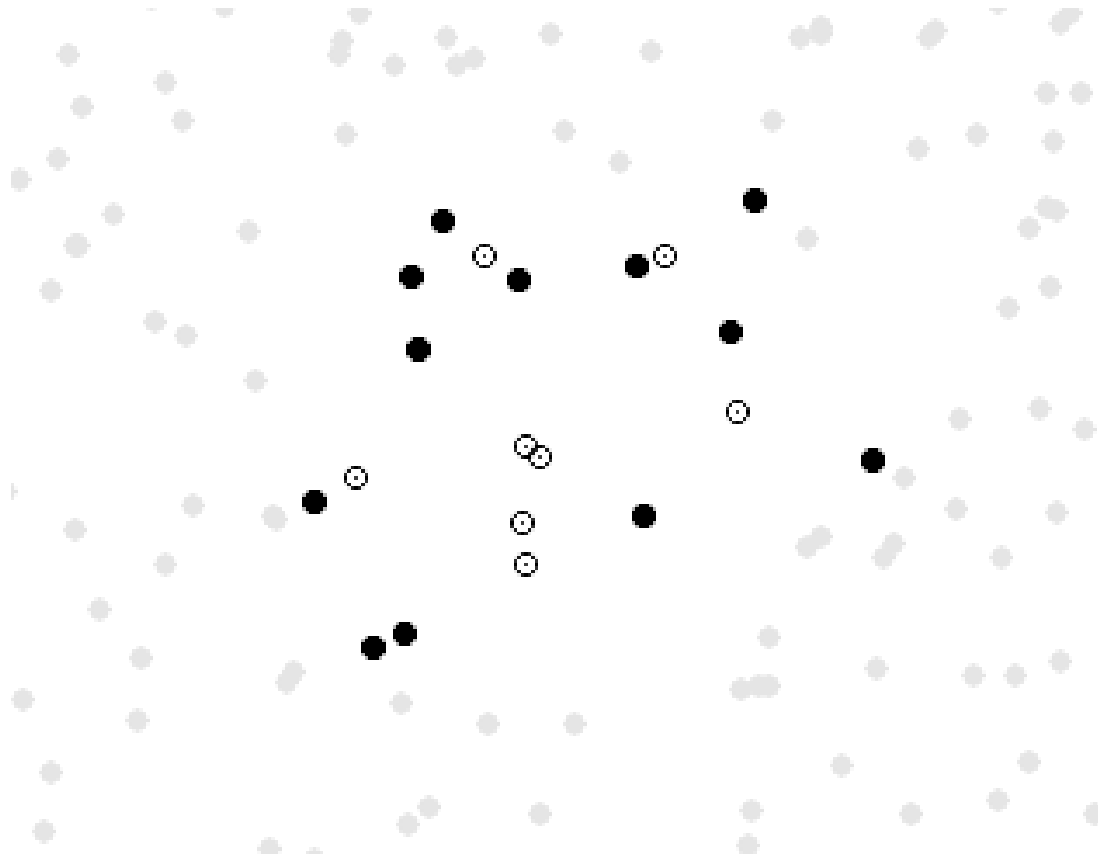
Analysis

- Complexity
 - Time : $O(|P|\log|P|)$
 - Space : $O(|P|)$
- Avoid
 - pairwise comparison
 - operations for $|Q|$ dimensional data
- Easy to parallelize

Example



Example

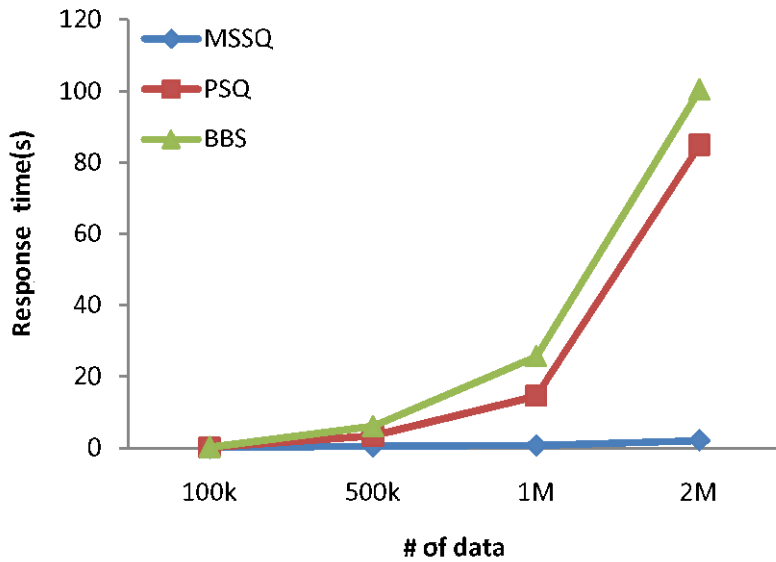


Experimental Evaluation

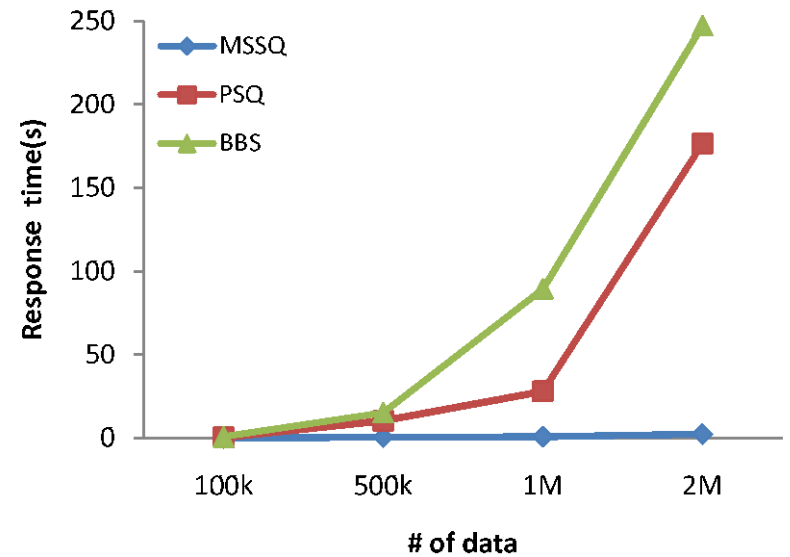
- Two base lines
 - PSQ : algorithm for skyline problems in general metric space.
 - BBS : algorithm for general skyline problems

Experimental Evaluation

- Synthetic datasets



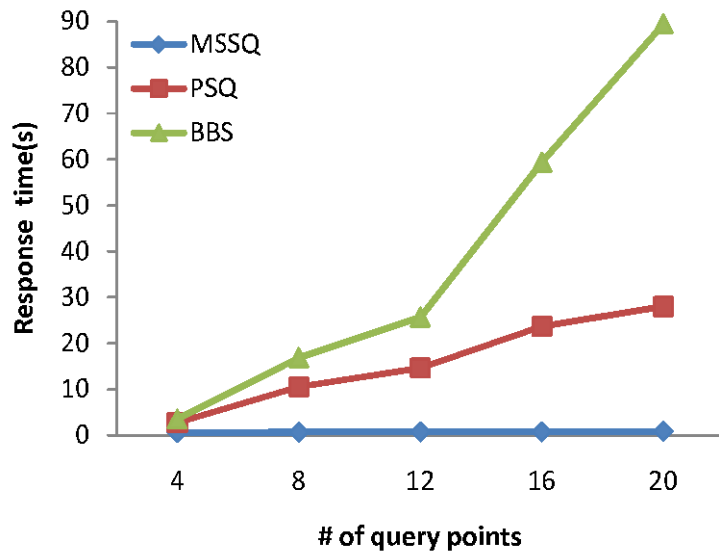
$|Q|=12$



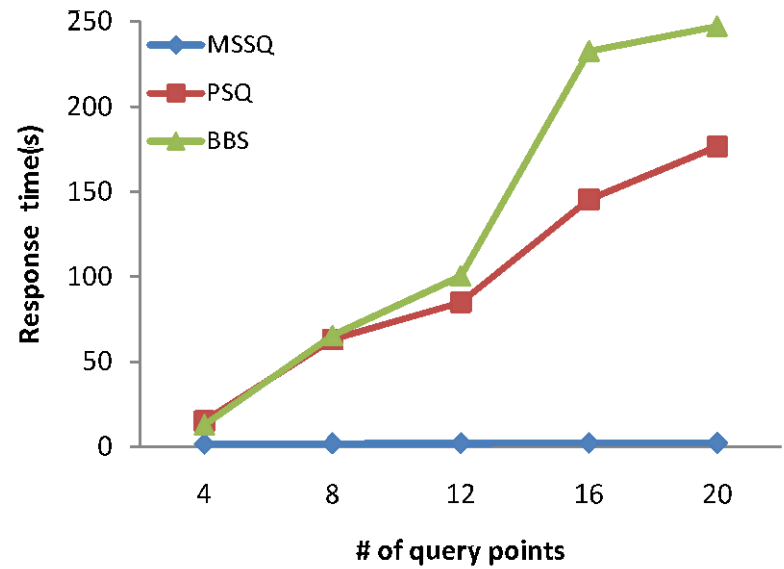
$|Q|=20$

Experimental Evaluation

- Synthetic datasets



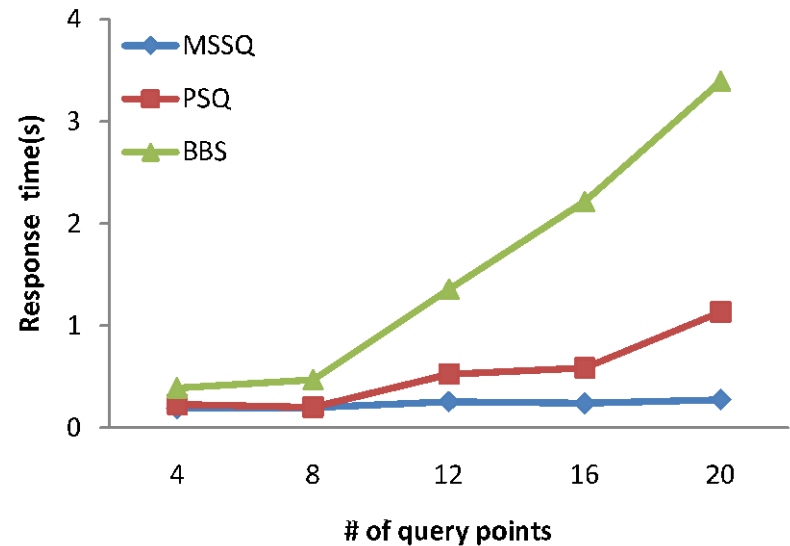
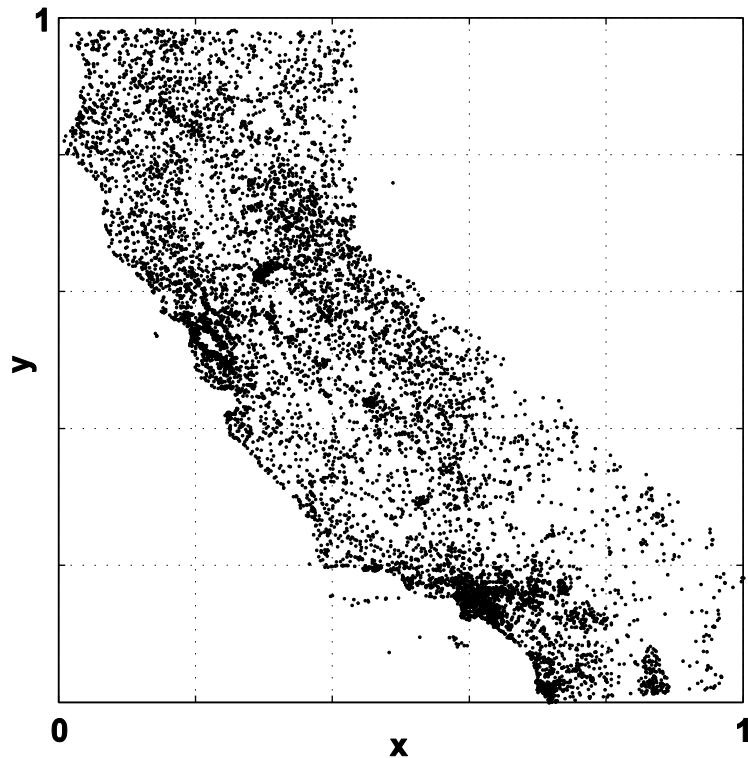
$|P|=1M$



$|P|=2M$

Experimental Evaluation

- POI datasets : California POI data 10k



Q&A